

## Kris Mas Solution Sheet

### Evaluation

Two periods: June and December

Discount rate: 20%/year – his rate for money, for his best project, his opportunity cost

Projects profits per unit sold is 3\$ = (15-12)

NPV =  $-20 + (12,000 \times 3)/1.1 \sim -20 + 32.4 = 12.4$  money in thousands

### Recognizing Uncertainty

Histograms differ because production is capacity constrained to 12,000 units.

NPV for each outcome indicated in expression below

### Value under Uncertainty

NPV =  $-20 +$  discounted expected value

$$= -20 + (1/1.0) [(0.1 \times 36) + (0.6 \times 30) + (0.3 \times 15)]$$

$$= -20 + (0.9) [3.6 + 18 + 4.5] = -20 + (0.9)[26.1] \sim 3.5$$

### Flexibility

The base decision tree shows 1 decision with 3 outcomes

The one with flexibility shows first decision augmented by cost of Tom in June (3)

And a second decision in December to keep Tom on if demand is 50,000, or not if demand is lower (either 5,000 or 10,000)

The Flexible decision has an extra cost of -3 at start, and a further cost of -3 IF there is the possibility ( $p = 0.1$ ) of boosting production from 12,000 to 50,000.

The Present Value of the incremental cash flows are:

$$\text{Change in NPV} = -3 + (p=0.1)(0.9)[-3 + (38 \times 3)] = -3 + (0.1)(0.9)[111] \sim -3 + 10 \sim 7$$

So NPV with Flexibility  $\sim 7 + 3.5 = 10.5$  – go for it

### EVPI

We Insert the Test as a decision before the Decision Tree for Flexible case

We do not give it a cost – we assume that we have it and see how much it is worth

Then we decide how much to pay for actual test (or consultancy) -- which isn't perfect

Perfect test has 2 outcomes in this case:

1) 10% chance that sales = 50,000 – if so go for it

$$\text{NPV in that case} = (0.1)[-23 (=20 + \text{Tom}) + (0.9)[(50 \times 3) - 3(\text{more Tom})]] \\ = (0.1)[-23 + (0.9)[147]] = 0.1(109.3) \sim 10.9$$

2) or 90% of either other two possibilities, whose net present value we calculated first

$$\text{So NPV in the "not 50,000" case is} = (0.9)[-23 + (0.9)[(0.6 \times 30) + (0.3 \times 15)]] \\ = (0.9)[-23 + (0.9)[22.5]] - \text{which is negative}$$

So, if you knew in advance that you couldn't get the 50,000, you would NOT go forward with project, and avoid the downside.

$$\text{EVPI} = \text{value after perfect test} - \text{value without} = 10.9 - 10.5 = 0.4$$

No way additional info worth the 2,000\$

I hope I didn't make an arithmetic mistake while typing.

Focus on the rationale of what needs to be done (as I done in grading tests!)

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