

# Lecture 17: Out-of-distribution generalization

Speaker: Sara Beery



Left: Courtesy of Mannion et al. Used under CC BY. Right: Courtesy of Sara Beery. Used under CC BY.



# Machine Learning: A Success Story



Image Classification

Input sentence:	Translation (PBMT):	Translation (GNMT):	Translation (human):
李克強此行將啟動中加總理年度對話機制，與加拿大總理杜魯多舉行兩國總理首次年度對話。	Li Keqiang premier added this line to start the annual dialogue mechanism with the Canadian Prime Minister Trudeau two prime ministers held its first annual session.	Li Keqiang will start the annual dialogue mechanism with Prime Minister Trudeau of Canada and hold the first annual dialogue between the two premiers.	Li Keqiang will initiate the annual dialogue mechanism between premiers of China and Canada during this visit, and hold the first annual dialogue with Premier Trudeau of Canada.

Machine Translation



Strategy Games

Image removed to copyright restrictions.

Realistic Image Generation



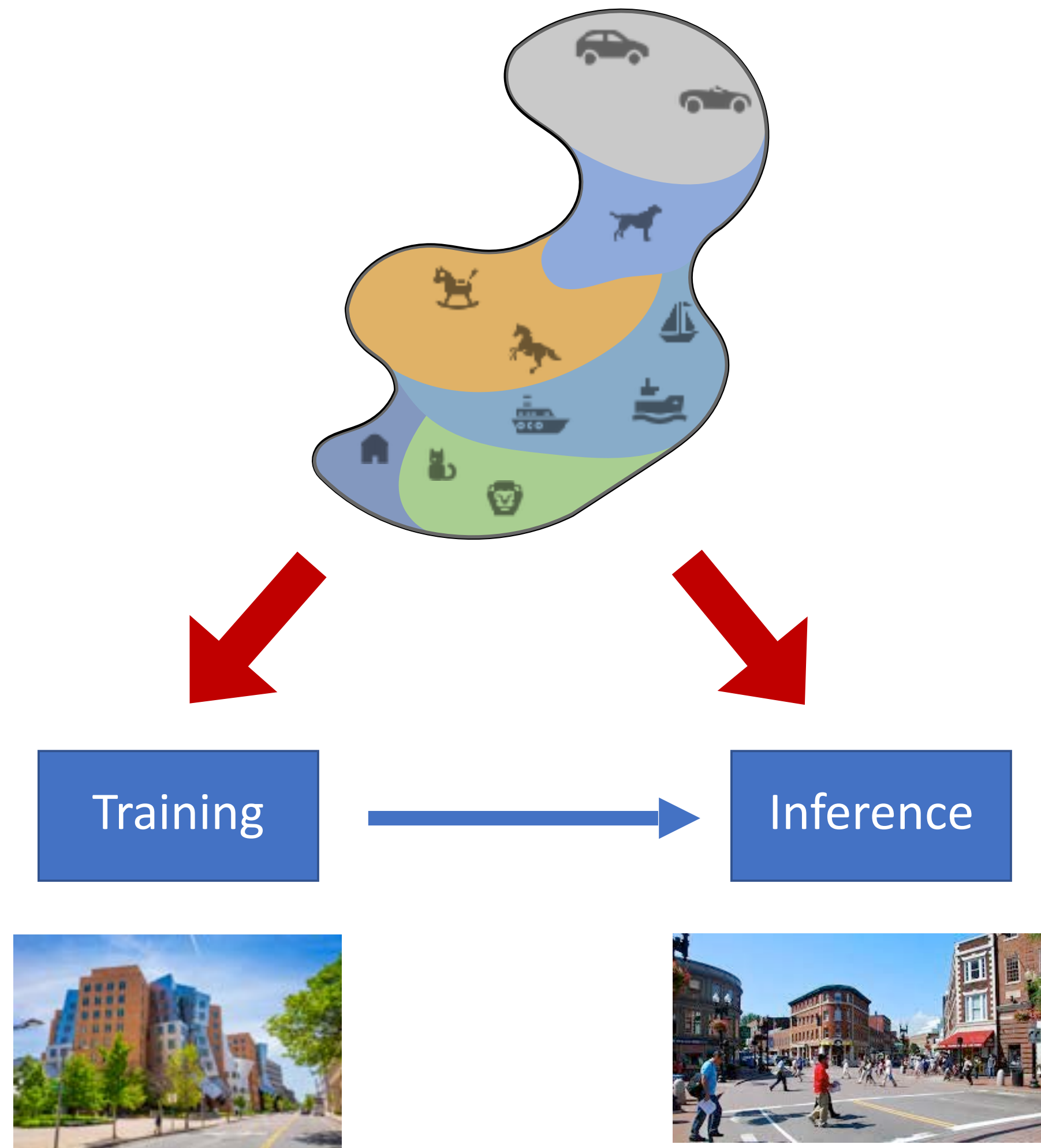
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Robotic Manipulation

Are ML systems really ready for the real world?



# Standard ML setting



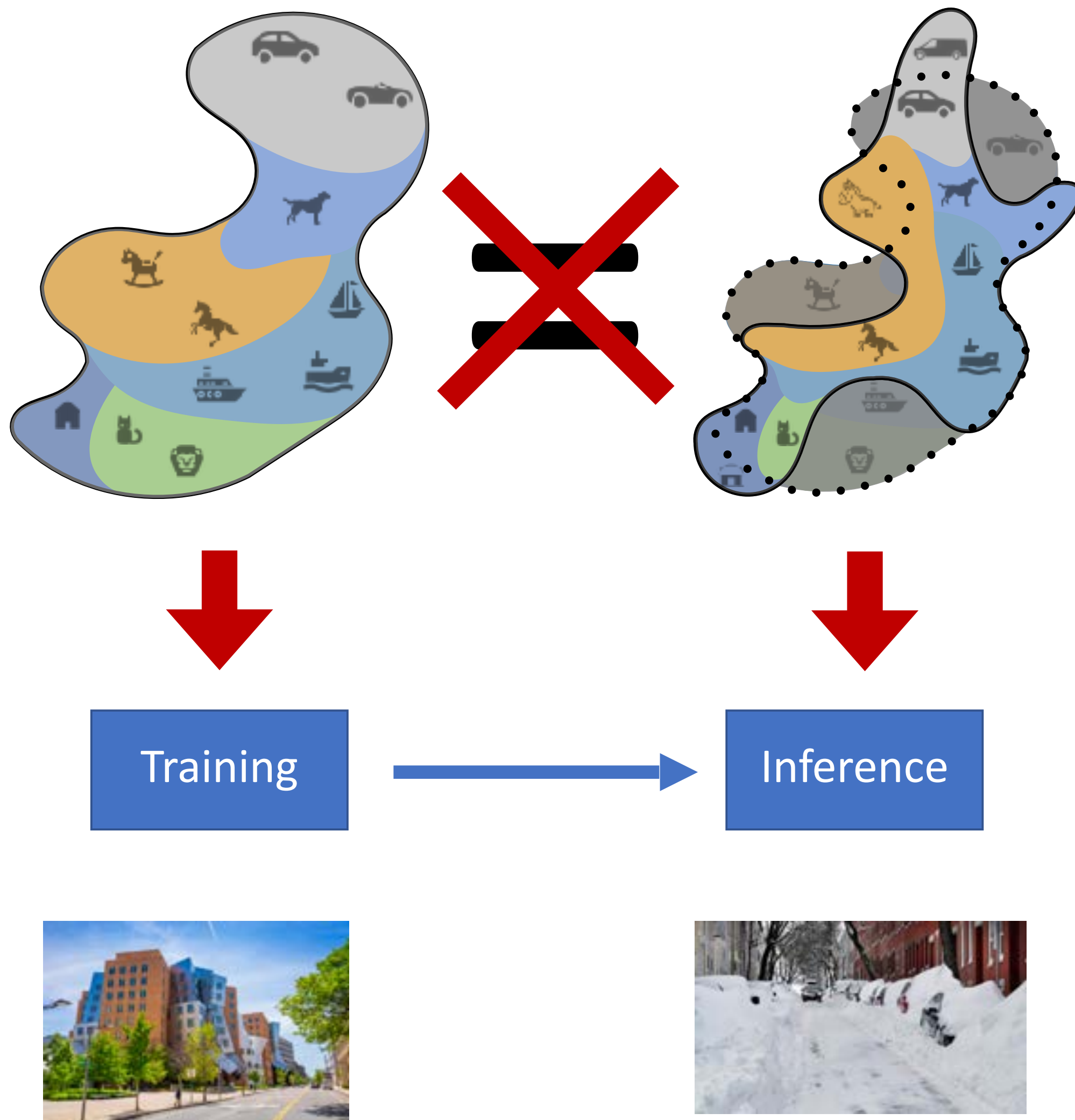
training distribution  
=  
test distribution

# ... vs the real world

deploy model on data from a different distribution

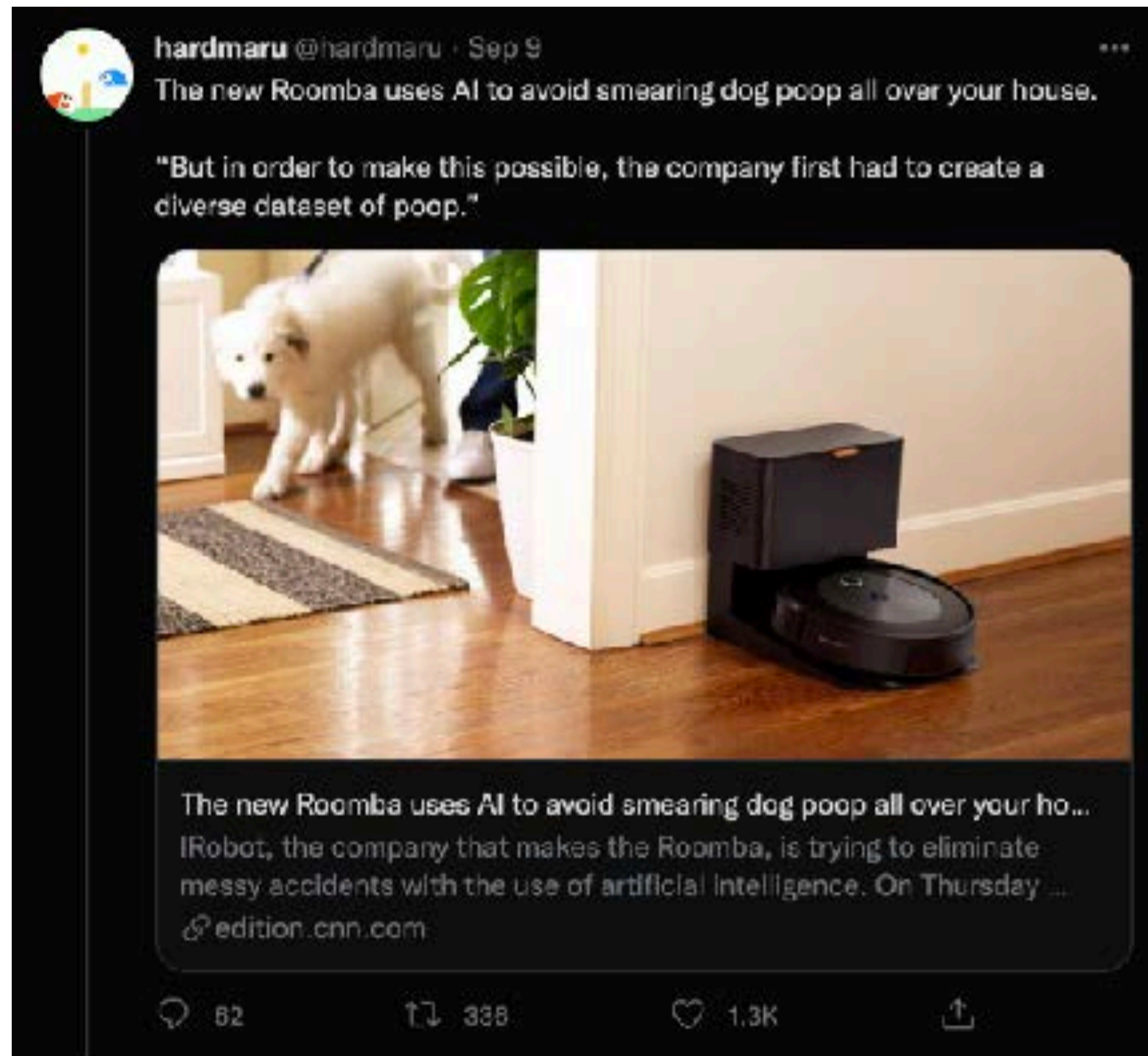
e.g.:

- perturbed data
- different label distribution
- other shifts (sequence/graph size, weather, country/city, source of measurement,...)





# What can go wrong?





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## Concrete Problems in AI Safety

---

**Dario Amodei\***  
Google Brain

**Chris Olah\***  
Google Brain

**Jacob Steinhardt**  
Stanford University

**Paul Christiano**  
UC Berkeley

**John Schulman**  
OpenAI

**Dan Mane**  
Google Brain

might serve a benchmarking role similar to that of the bAbI tasks [163], with the eventual goal being to develop a single architecture that can learn to avoid catastrophes in all environments in the suite.

## 7 Robustness to Distributional Change

All of us occasionally find ourselves in situations that our previous experience has not adequately prepared us to deal with—for instance, flying an airplane, traveling to a country whose culture is very different from ours, or taking care of children for the first time. Such situations are inherently

# Outline for today

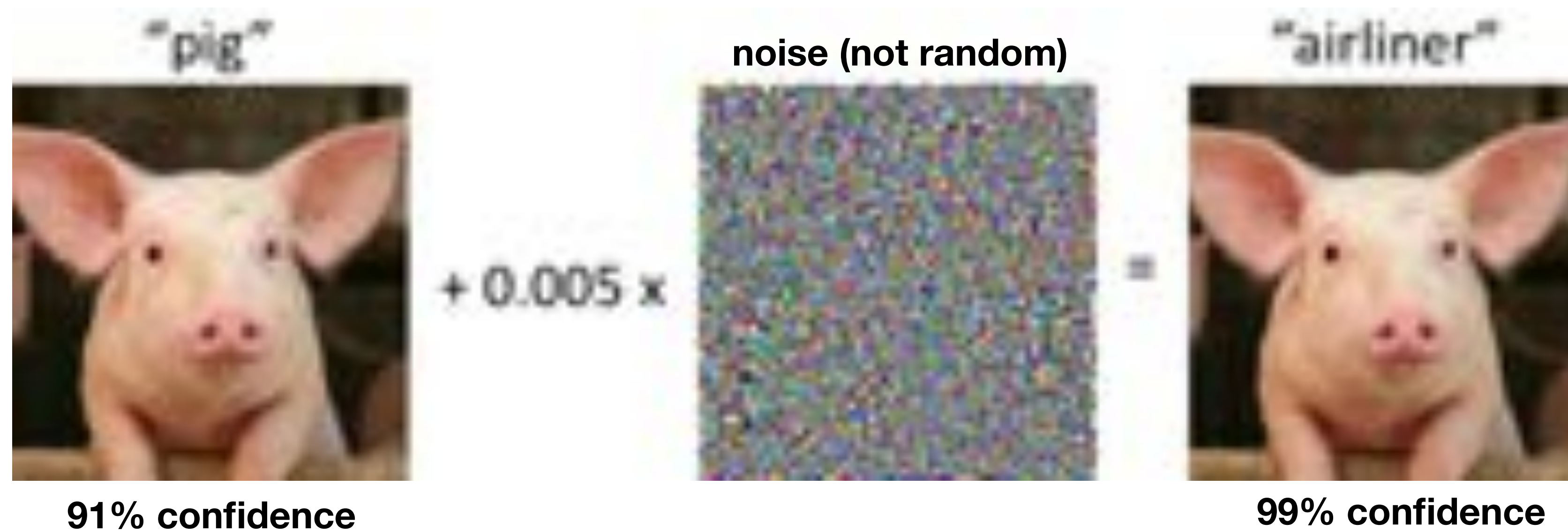
- Adversarial examples and training: small perturbations
- Distribution Shifts



# Adversarial examples



# Adversarial examples



- ML model predictions are (mostly) accurate but can be brittle

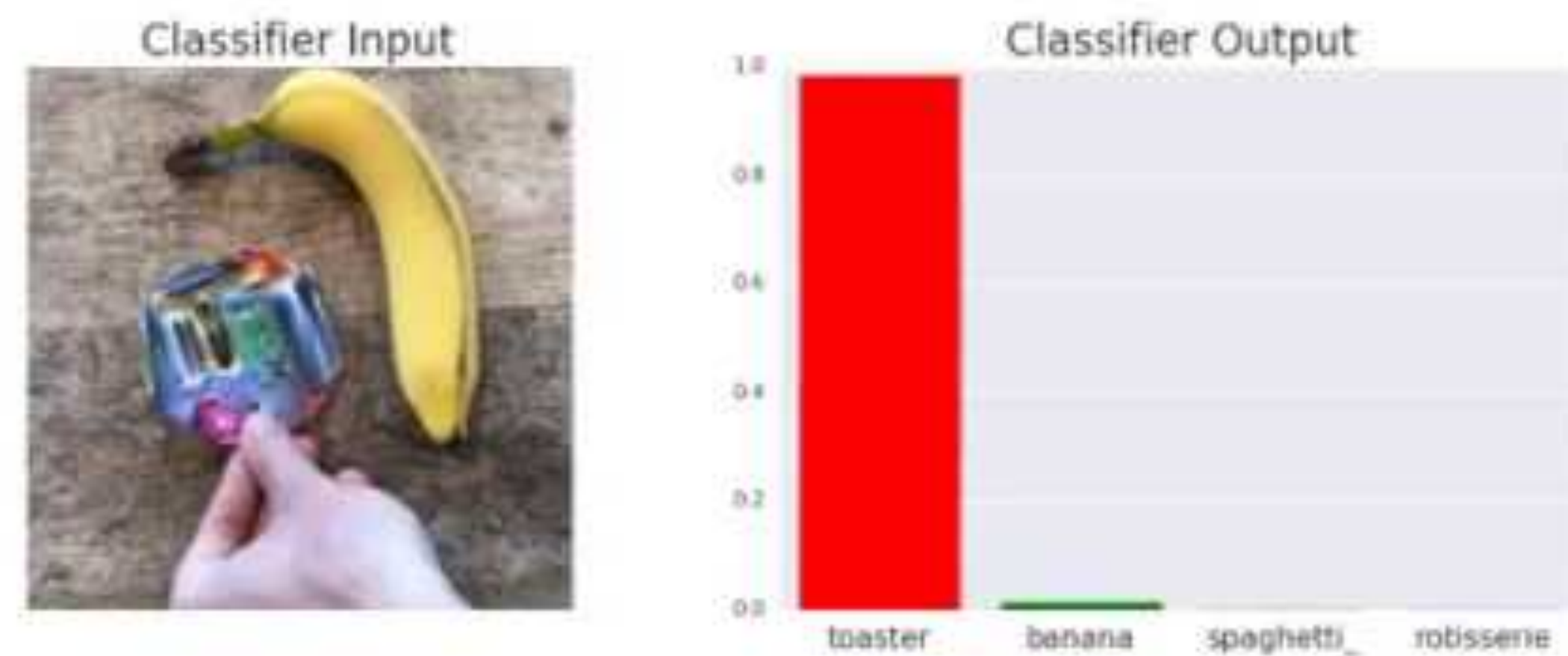


# Adversarial examples





# Adversarial stickers





# Adversarial stickers

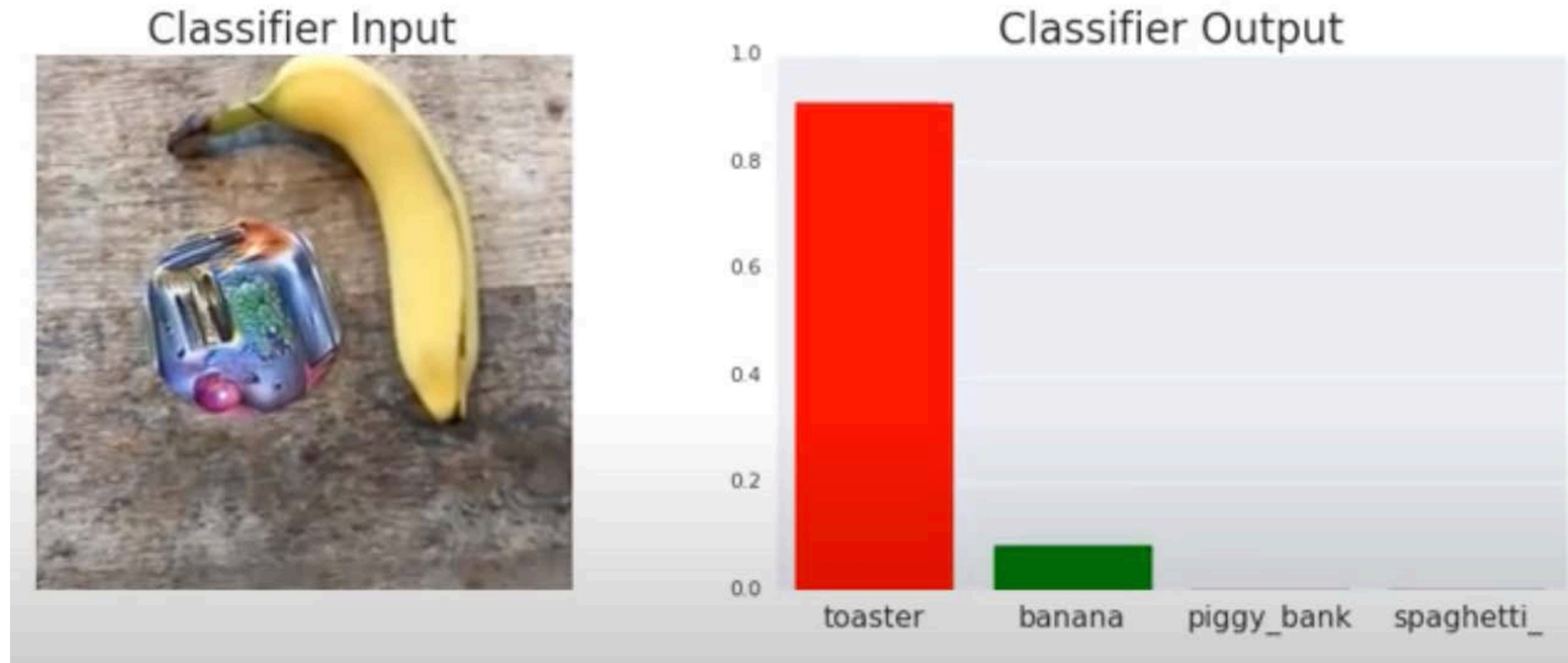




# Adversarial stickers



# Adversarial stickers





# Adversarial examples 3D-printed





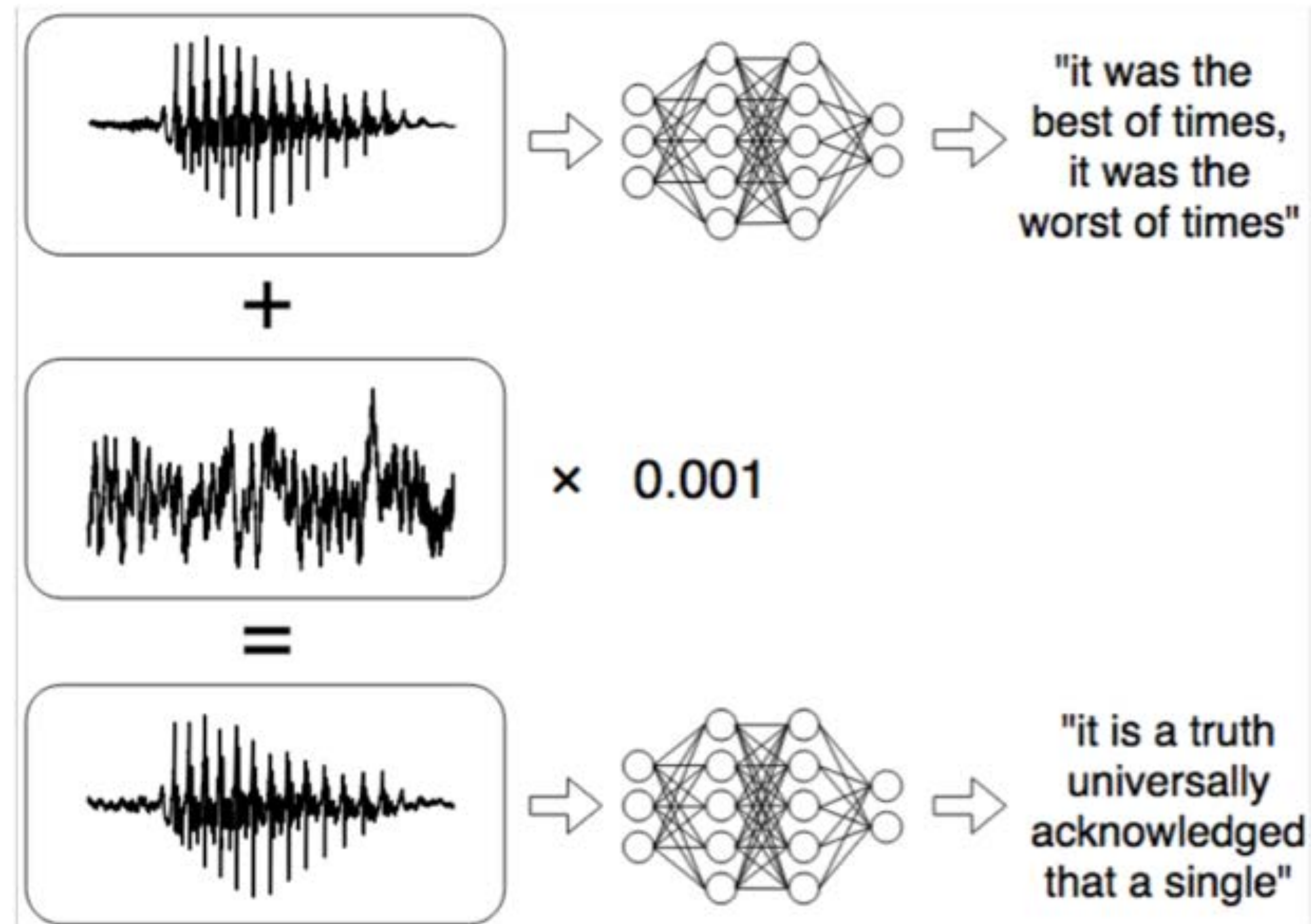
# Adversarial examples 3D-printed



■ classified as turtle      ■ classified as rifle  
■ classified as other



# Speech recognition example

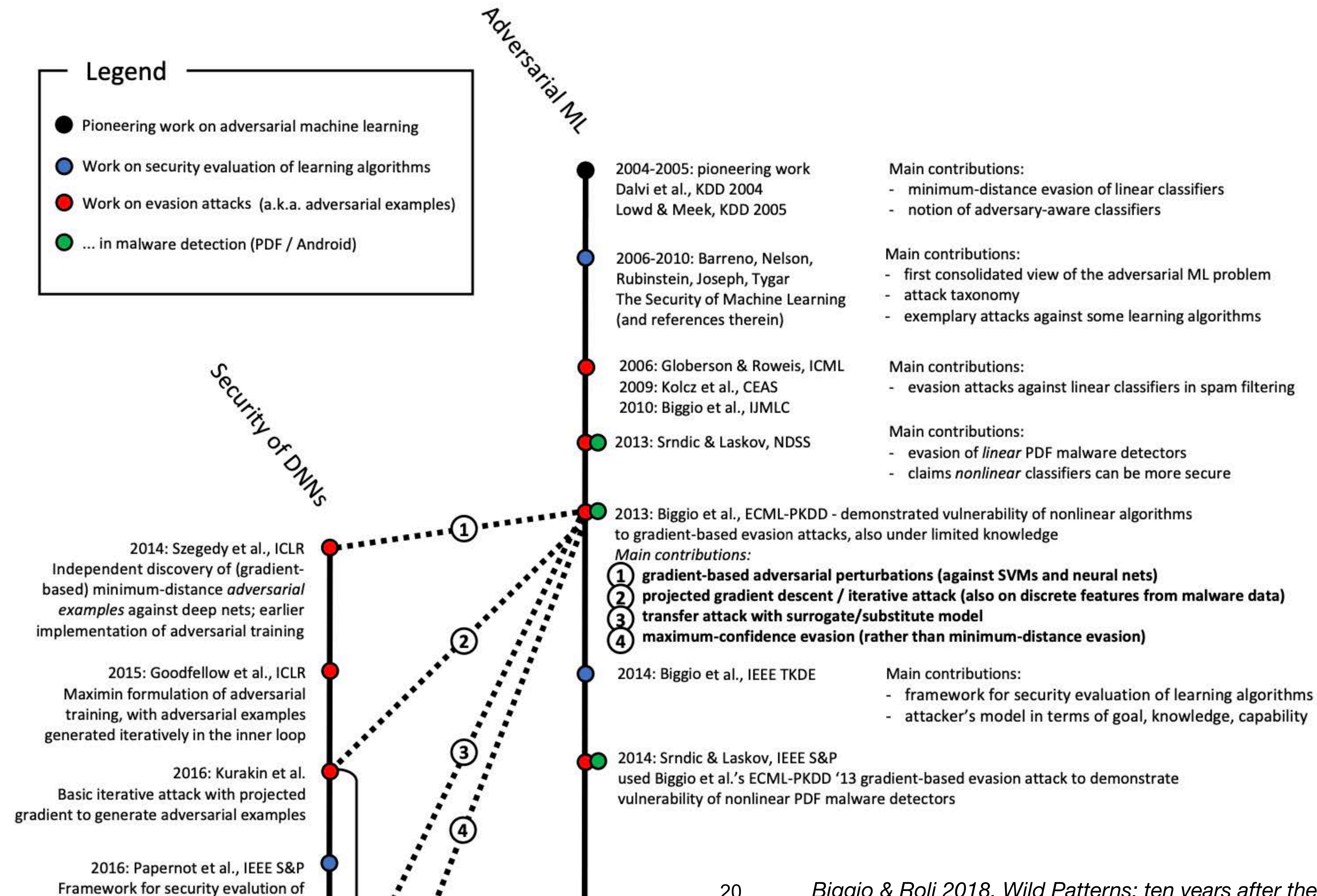


# Hmmm....

- Are our models completely useless?
- Why does this happen?
- Can one prevent it?



# History of adversarial examples / brittleness

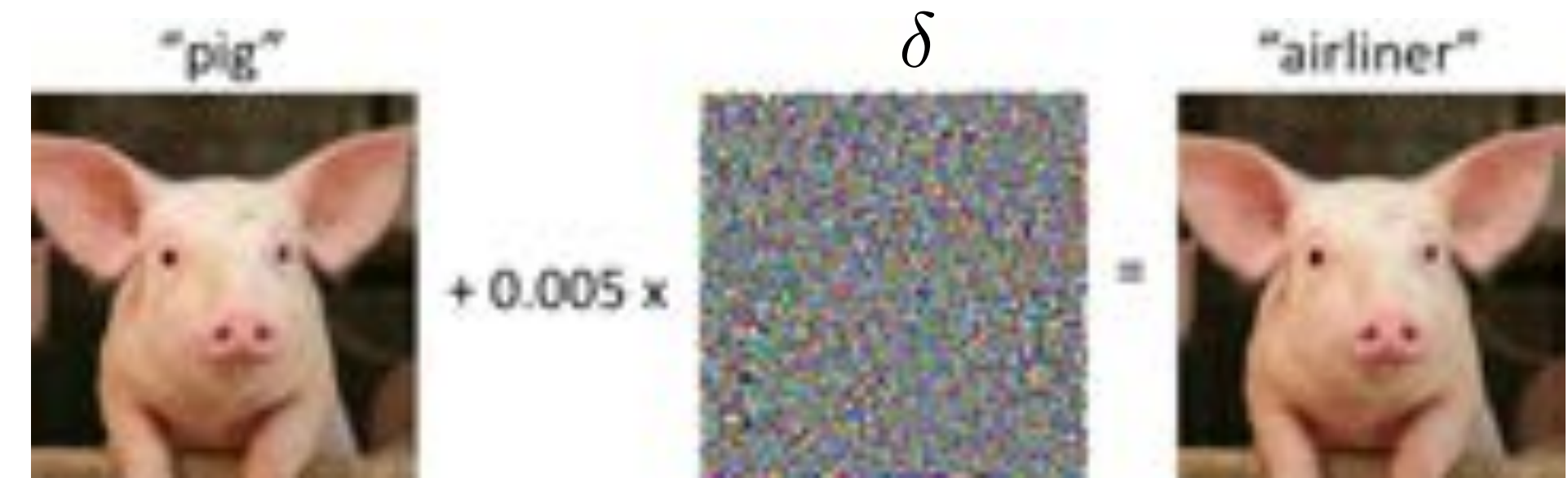


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# How do you create an adversarial example?

- want: small perturbation that does not change meaning to a human, but to ML model



- model outputs  $P_{\theta}(y | \mathbf{x})$  (softmax)

- adversarial example:

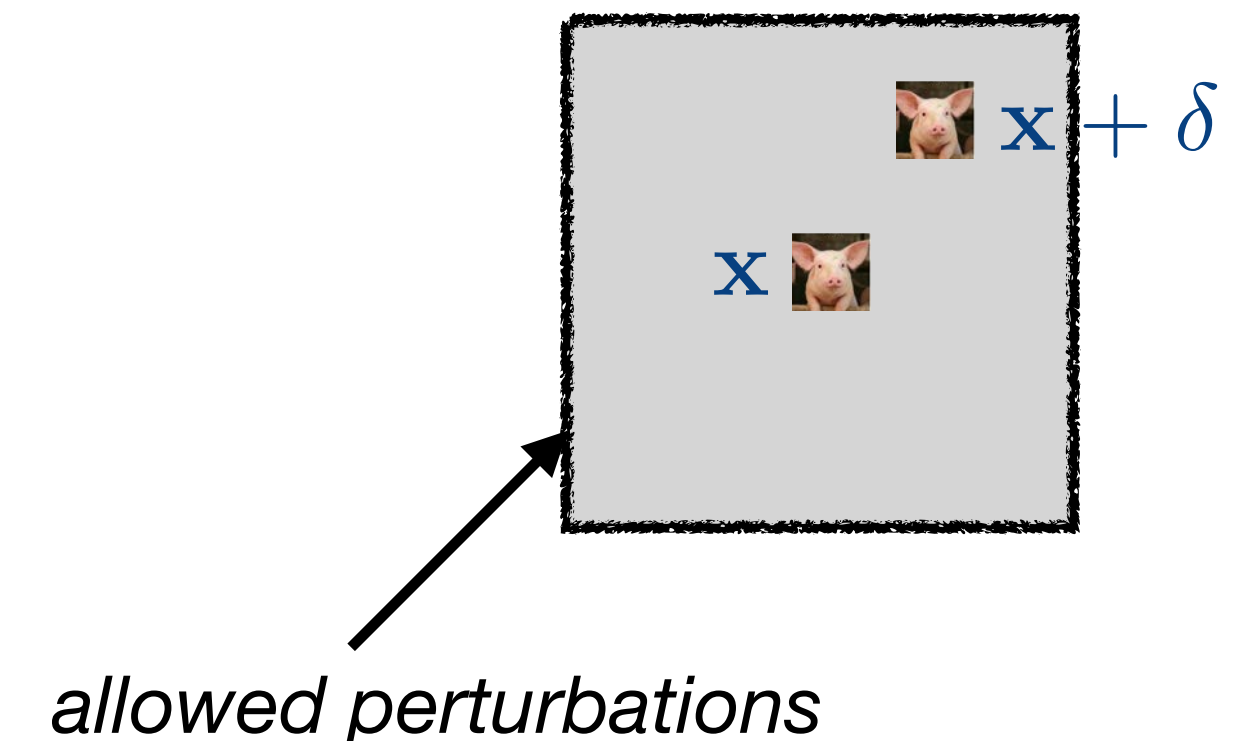
$$\max_{\delta \in \Delta} P_{\theta}(y_{\text{target}} | \mathbf{x} + \delta)$$

$\delta \in \Delta$  is a **small perturbation, e.g.**

$y_{\text{target}}$  is a **wrong class ("airliner")**

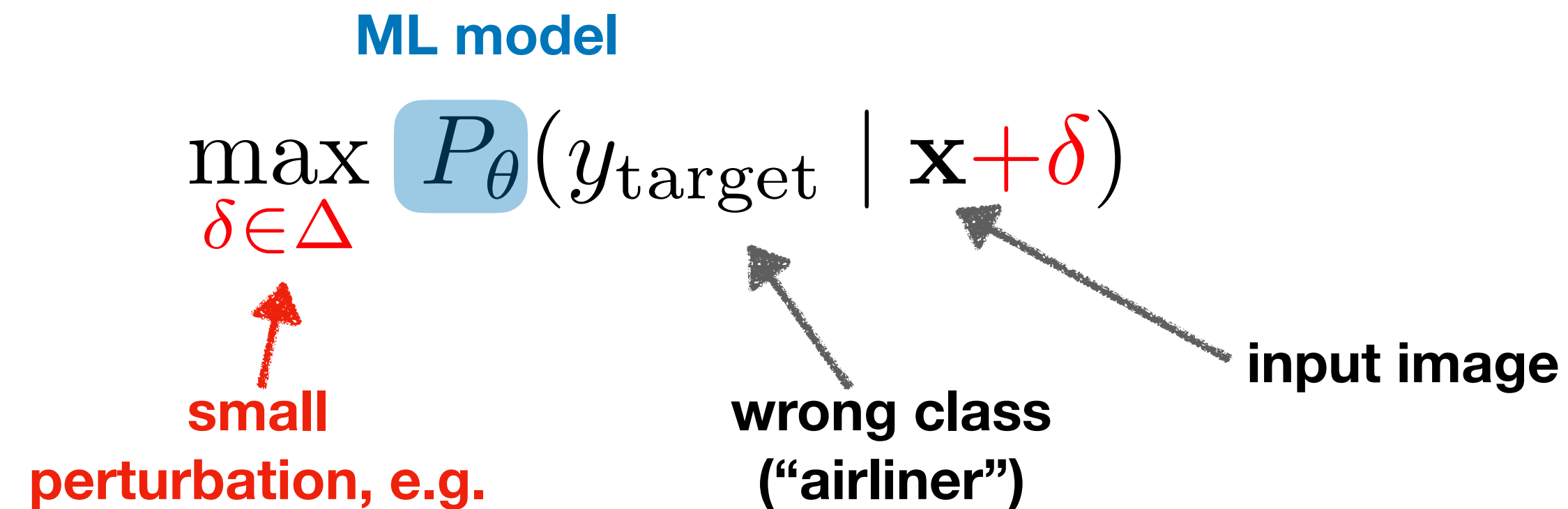
$\mathbf{x}$  is the **input image**

$$\Delta = \{\delta \in \mathbb{R}^d \mid \|\delta\|_{\infty} < \epsilon\}$$

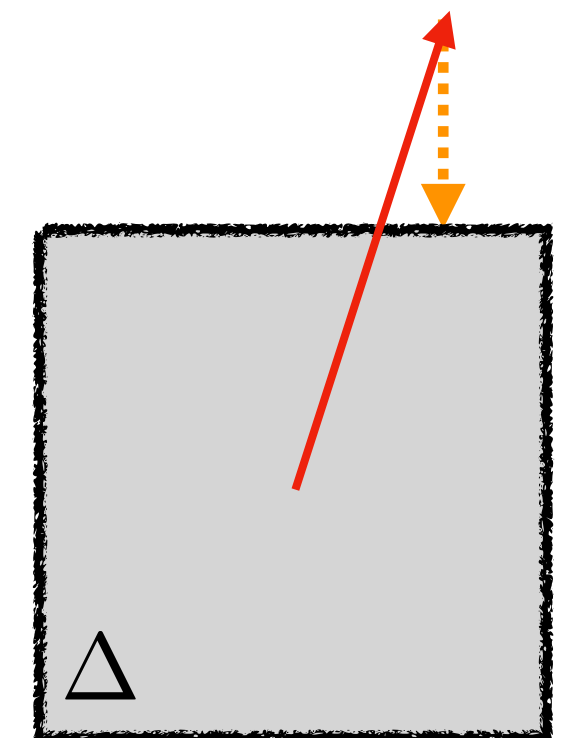




# How to find an adversarial example?



- e.g. Projected gradient ascent (we update data perturbation  $\delta$ ):
  - take a step in the direction of the gradient:
$$\delta^{(t+1)} = \delta^{(t)} + \eta \cdot \nabla_{\delta} P_{\theta}(y_{\text{target}} \mid \mathbf{x} + \delta)$$
  - project the result back into the feasible set  $\Delta$
  - repeat steps 1 & 2



# How to “defend” against adversarial examples?

Recall:

- Adversarial example                      versus                      standard training:

$$\max_{\delta \in \Delta} \text{Loss} \left( f_{\theta}(\mathbf{x} + \delta), y \right)$$

$$\min_{\theta} \text{Loss} \left( f_{\theta}(\mathbf{x}), y \right)$$



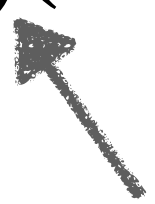
# How to “defend” against adversarial examples?

- **Standard training:**

via (stochastic) gradient descent

$$\min_{\theta} \frac{1}{n} \sum_{i=1}^n \text{Loss}(f_{\theta}(\mathbf{x}^{(i)}), y^{(i)})$$

neural network



- **Adversarial training / robust optimization:**

$$\min_{\theta} \frac{1}{n} \sum_{i=1}^n \max_{\delta \in \Delta} \text{Loss}(f_{\theta}(\mathbf{x}^{(i)} + \delta), y^{(i)})$$

*“adaptive data augmentation”*

# Adversarial training with stochastic gradient descent

$$\min_{\theta} \frac{1}{n} \sum_{i=1}^n \max_{\delta \in \Delta} \text{Loss}(f_{\theta}(\mathbf{x}^{(i)} + \delta), y^{(i)})$$

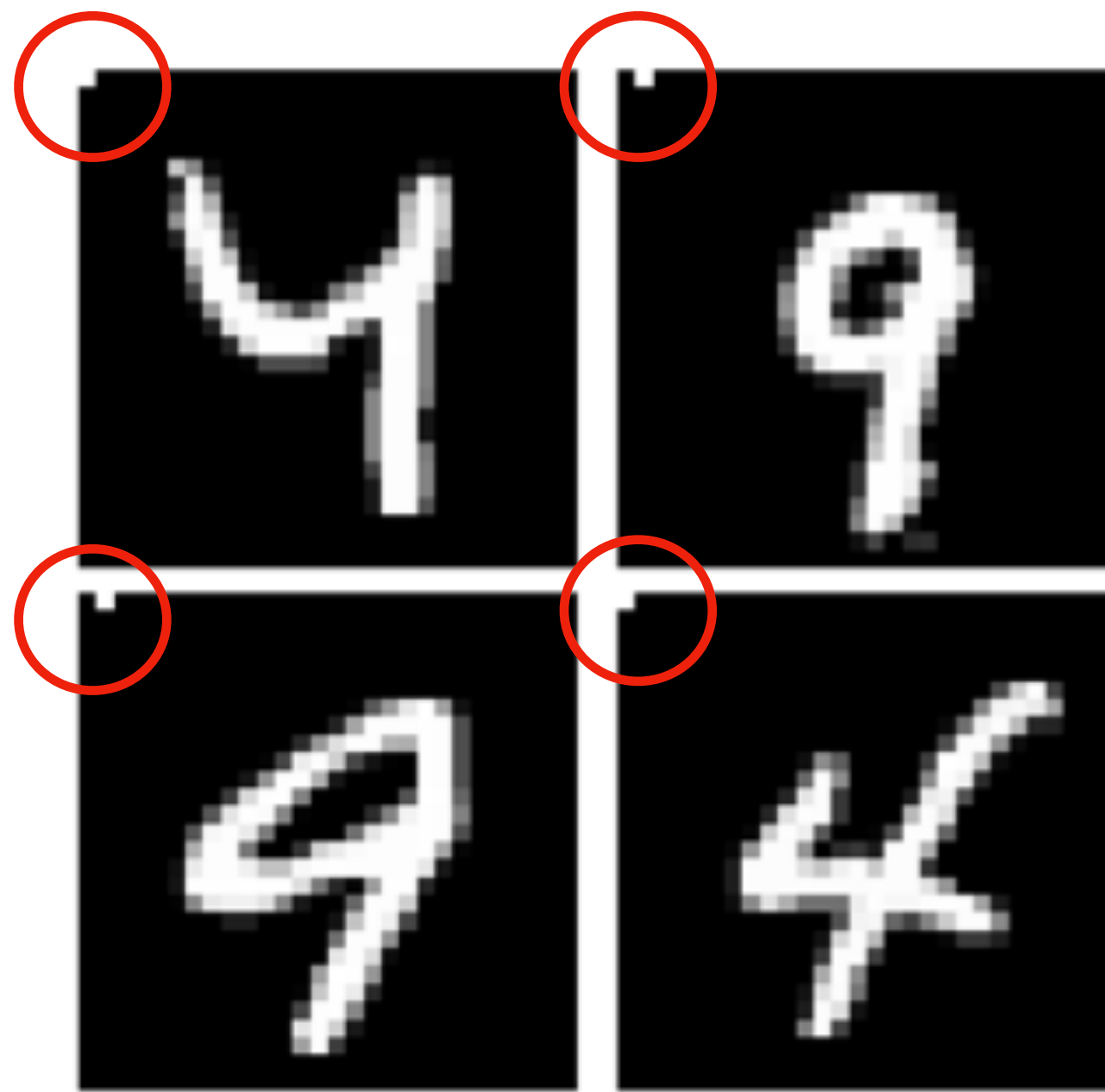
repeat until convergence:

1. sample a data point  $(\mathbf{x}, y)$
2. compute the optimal adversarial perturbation  $\delta^*$  (approximately)
3. compute the gradient  $g = \nabla_{\theta} \text{Loss}(f_{\theta}(\mathbf{x} + \delta^*), y)$
4. update  $\theta$  with the gradient  $g$

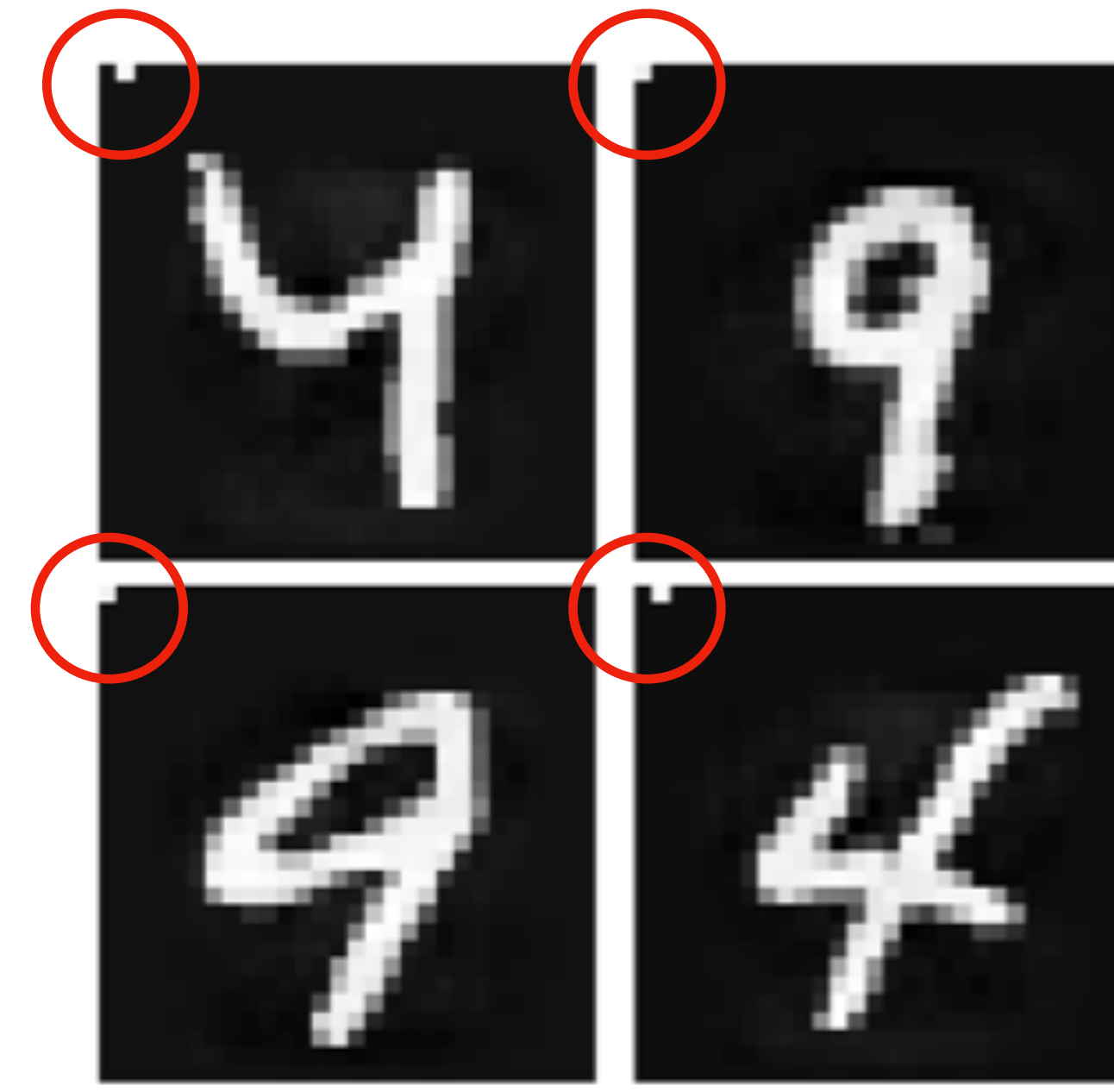


# What do adversarial examples tell us?

- something about the input “features” that are critical for the model’s decision
- Example:



**Training data:  
classify 4 vs 9**

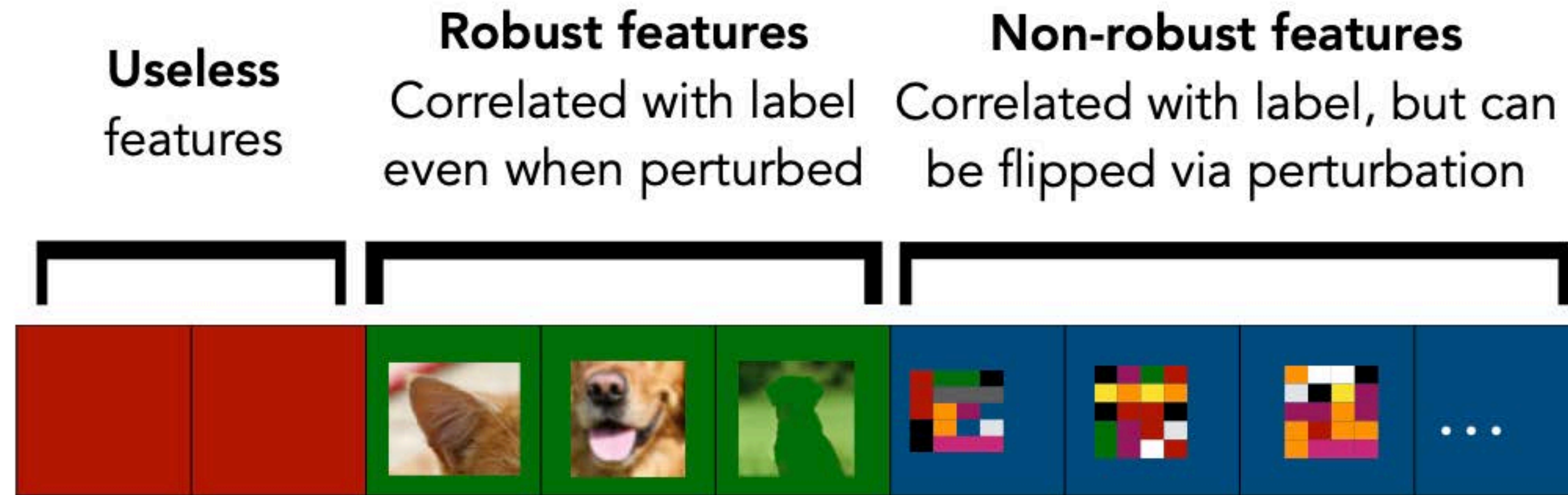


**Adversarial  
perturbations**

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*images: Hongzhou Lin*

# Predictive features



- Many features may be **correlated with the label** and hence predictive and help with accuracy, *beyond what humans would use*.

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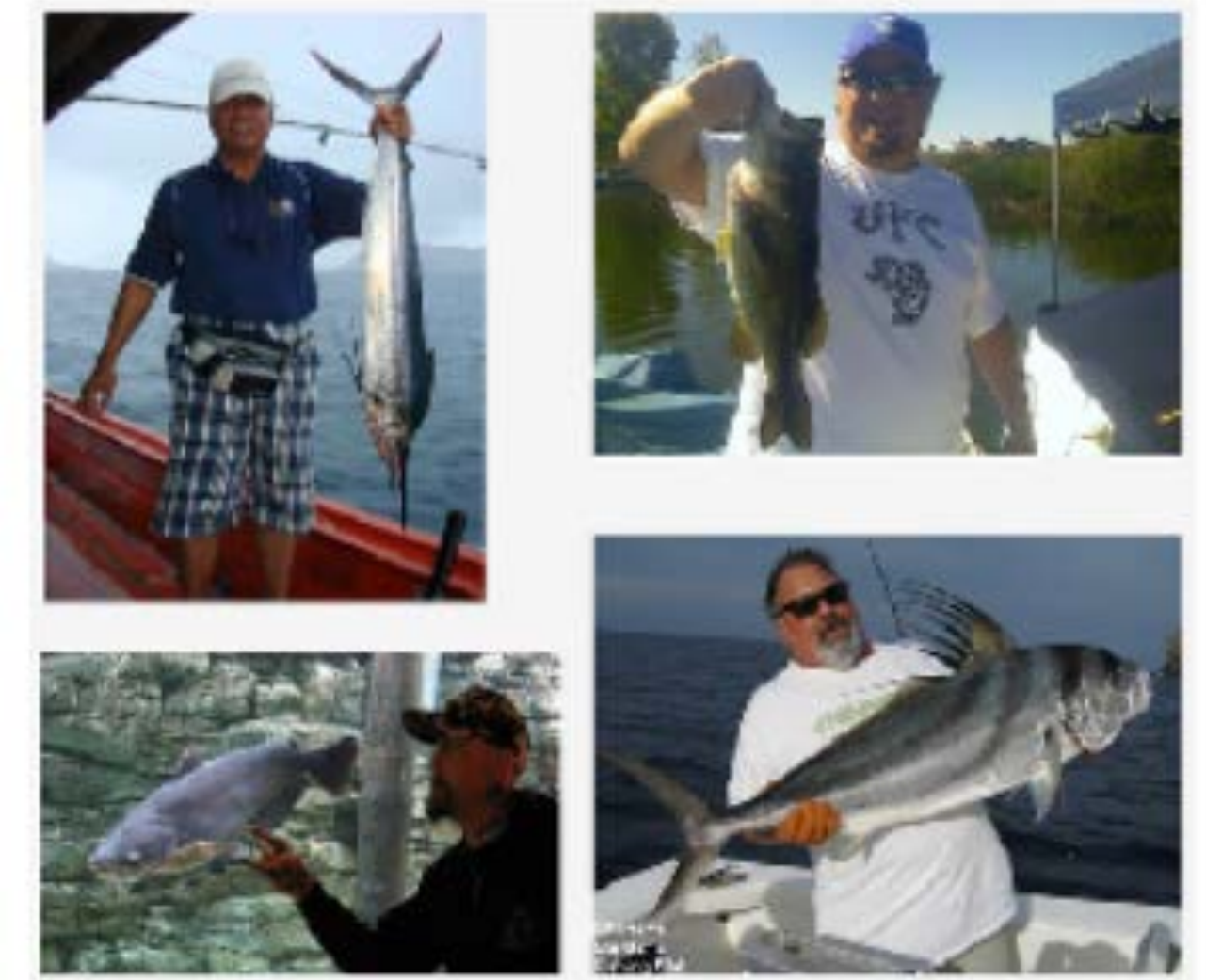
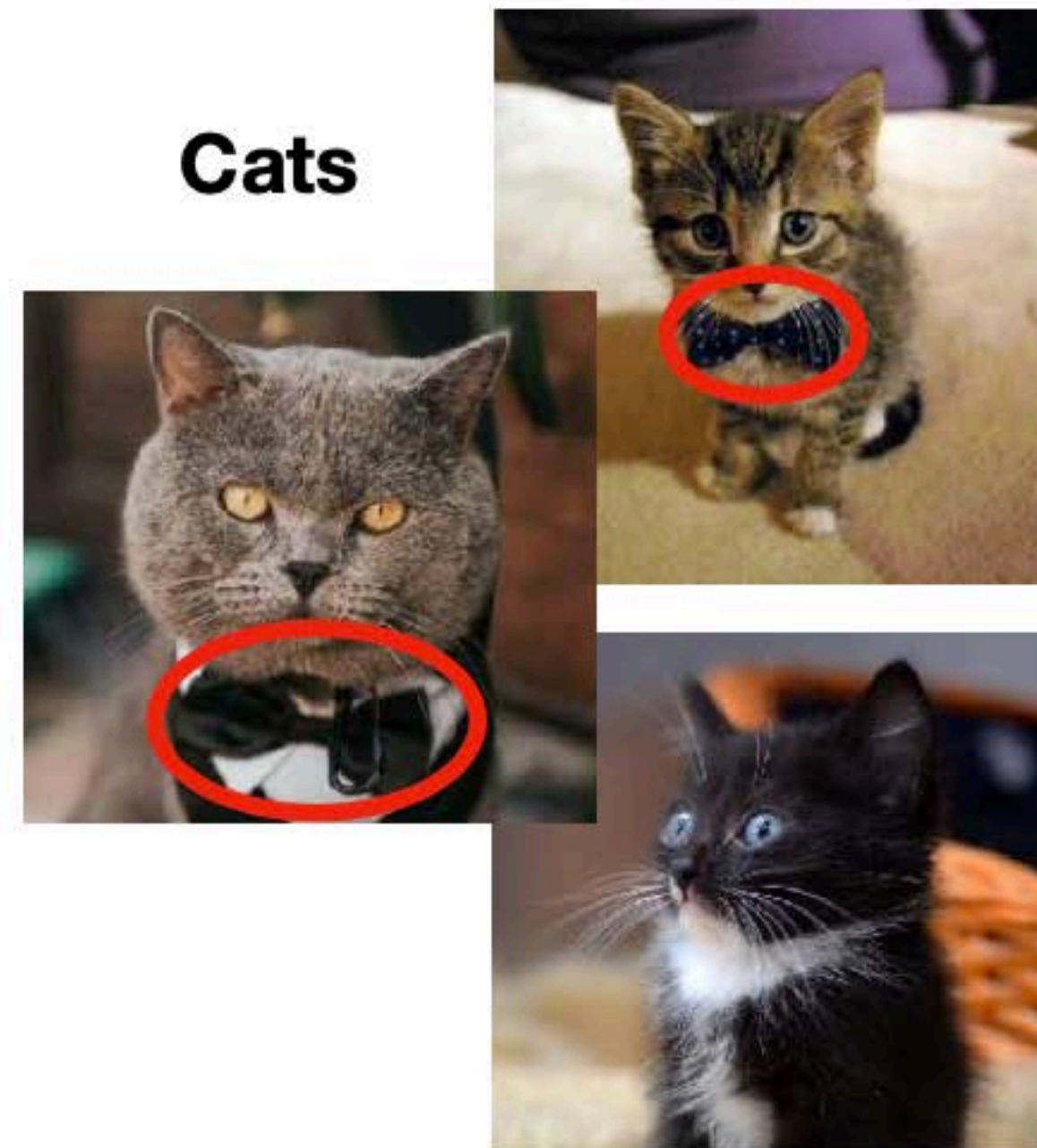
# Where do these correlations come from?

- Data

**Dogs**



**Cats**



“Fish” from the ImageNet training set

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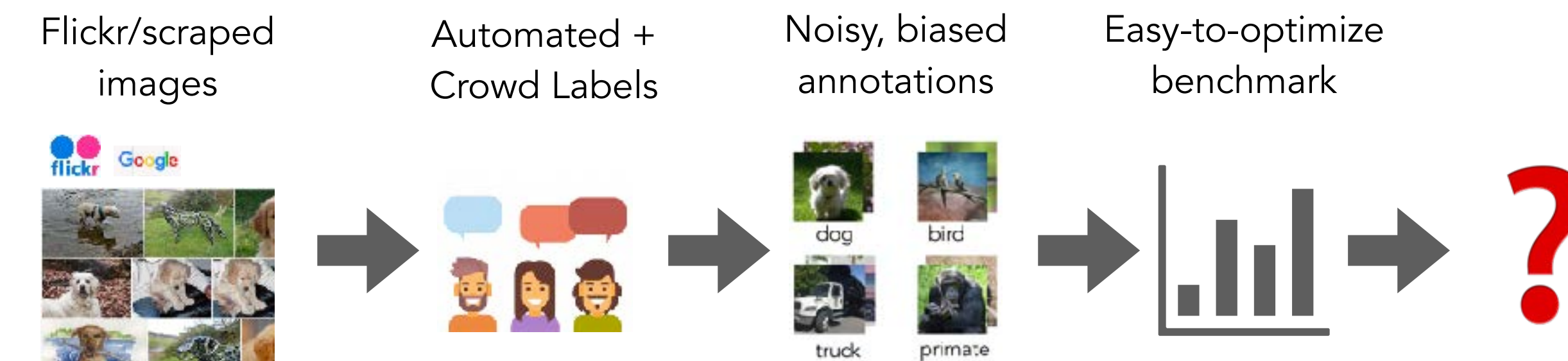
# Where do these correlations come from?

- ...and how we create datasets

## Ideal world:



## ~~Ideal~~ Real world:

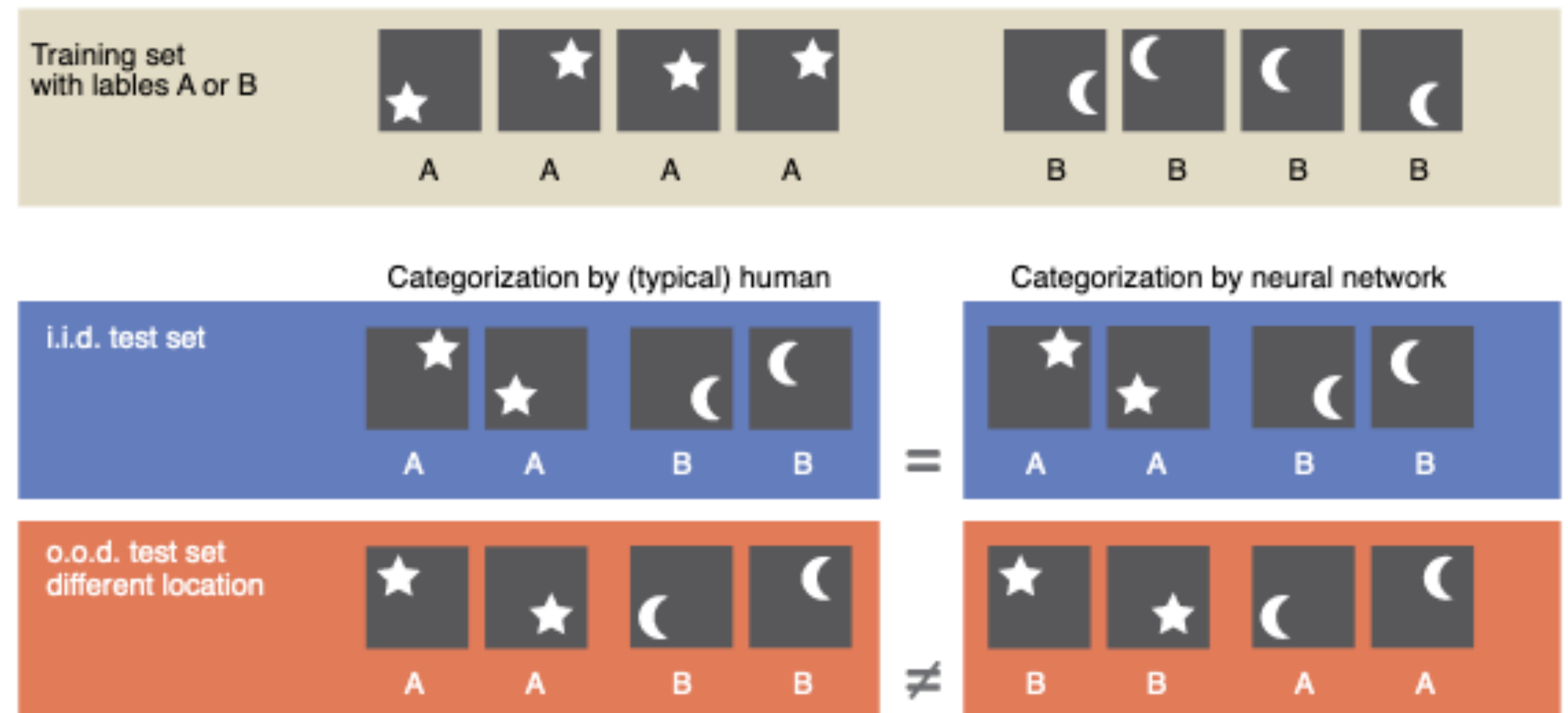


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# It's all "shortcuts"

- Shortcuts: features correlated with label in the training data, but not under realistic distribution shifts
- Models will use them and not generalize if features are no longer correlated



# It's all “shortcuts”

- Shortcuts: features correlated with label in the training data, but not under realistic distribution shifts
- Models will use them and not generalize if features are no longer correlated
- This is related to **data**, not models: ***adversarial examples transfer across models trained on the same dataset***



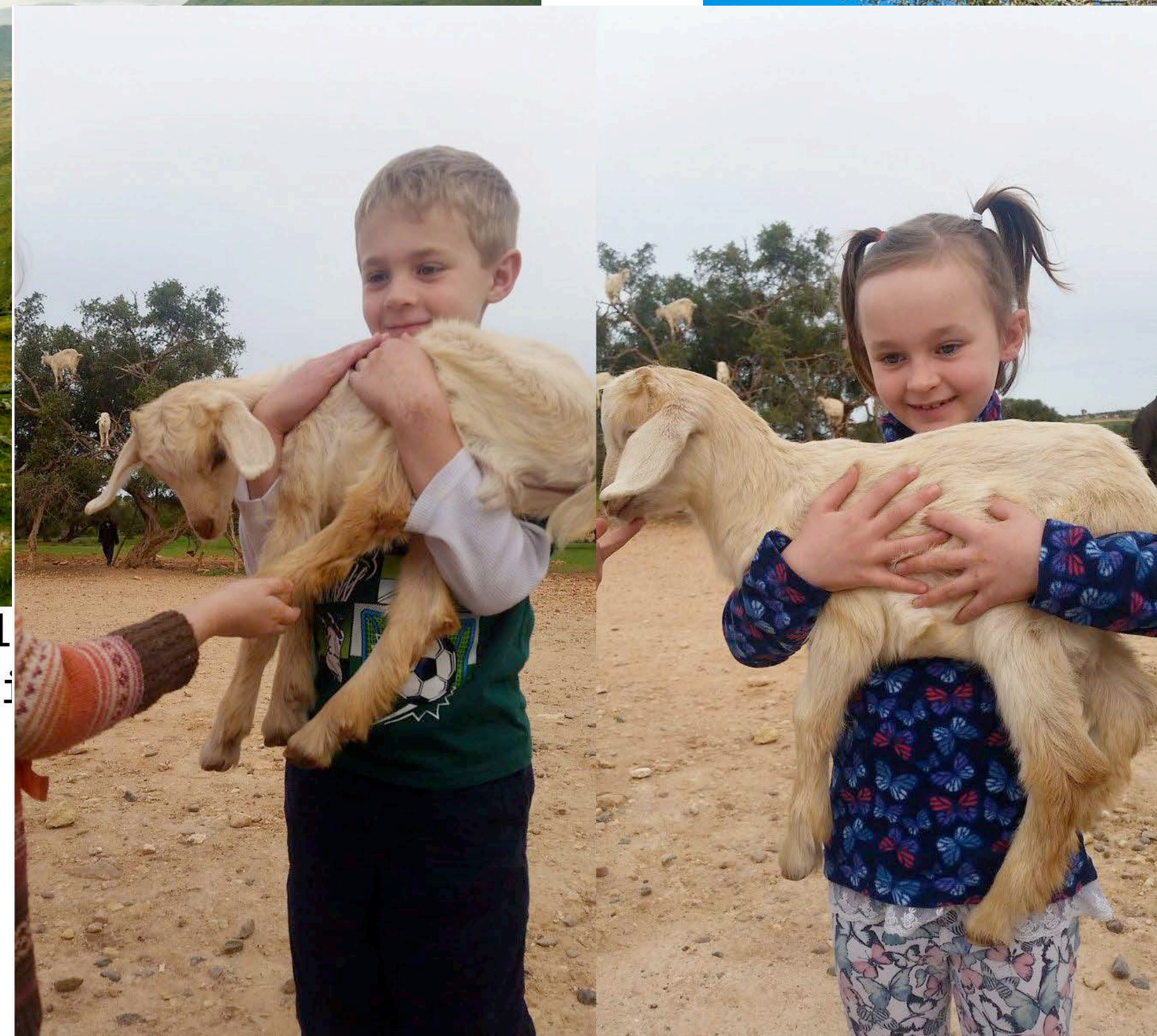
# What can these shortcuts look like?



A herd of sheep grazing on a mountain slope  
Tags: grazing, sheep, mountain



A flock of sheep standing on a tree  
Source: [www.flickr.com/photos/gratapictures](https://www.flickr.com/photos/gratapictures) - CC-BY-NC



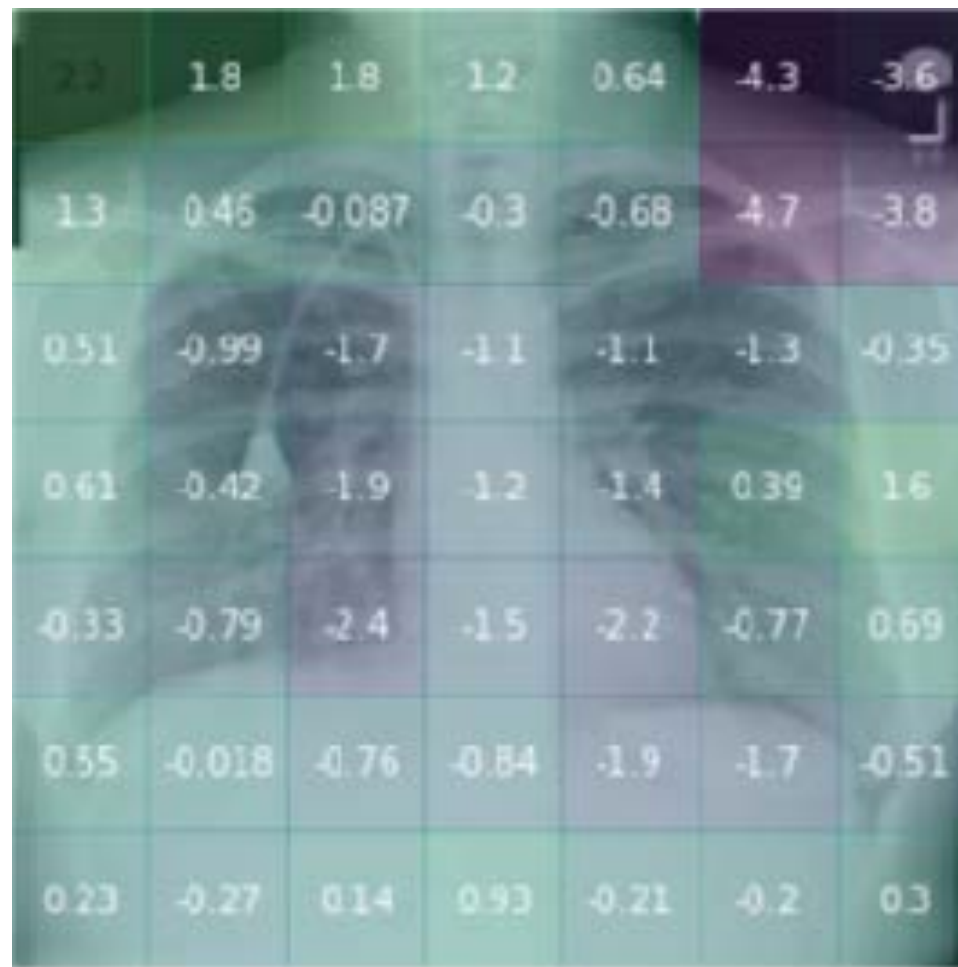
Left: A man is holding a dog in his hand  
Right: A woman is holding a dog in her hand  
Image: @SouperSarah

images: <https://www.aiweirdness.com/do-neural-nets-dream-of-electric-18-03-02/>

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# What can these shortcuts look like?



"CNNs were able to detect where an x-ray was acquired [...] and calibrate predictions accordingly."

[Zech et al. 2018]

"...if an image had a ruler in it, the algorithm was more likely to call a tumor malignant..."

[Esteva et al. 2017]



**not all predictive patterns are desirable**

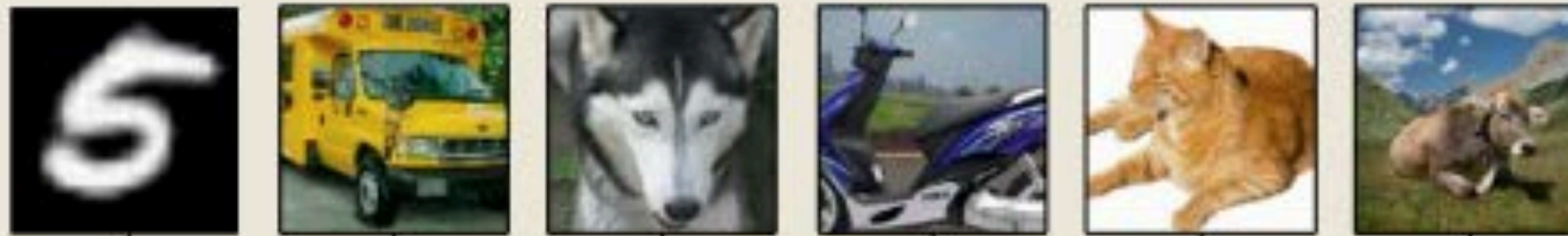
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# Many more...

**Same category for humans**  
but not for DNNs (intended generalization)

i.i.d.



Domain shift Wang 2018    Adversarial examples Szegedy 2013    Distortions Dodge 2019    Pose Alcorn 2019    Texture Geirhos 2019    Background Beery 2018

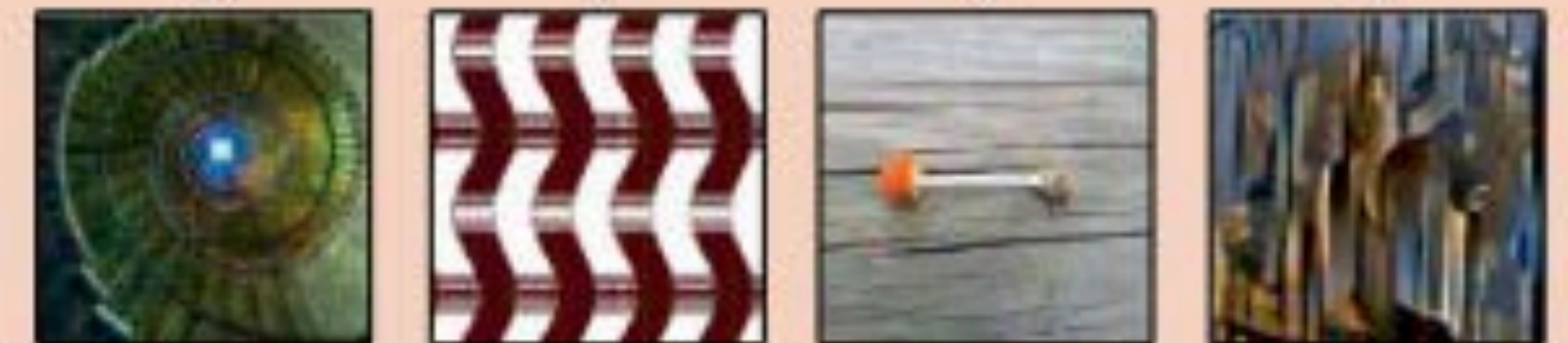


o.o.d.

**Same category for DNNs**  
but not for humans (unintended generalization)



Excessive invariance Jacobson 2019    Fooling images Nguyen 2015    Natural adversarials Hendrycks 2019    Texturized images Brendel 2019





# Transformers Learn Shortcuts to Automata

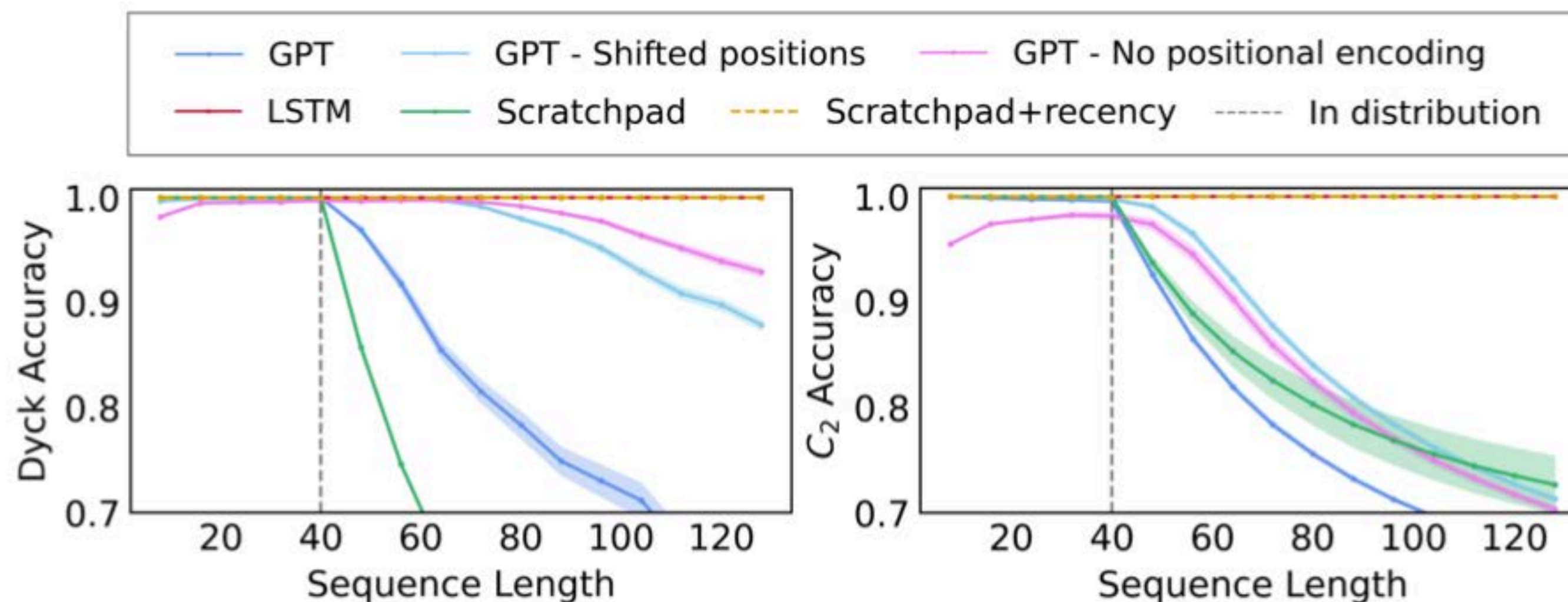
Bingbin Liu<sup>1\*</sup> Jordan T. Ash<sup>2</sup> Surbhi Goel<sup>2,3</sup> Akshay Krishnamurthy<sup>2</sup> Cyril Zhang<sup>2</sup>

<sup>1</sup>Carnegie Mellon University    <sup>2</sup>Microsoft Research NYC    <sup>3</sup>University of Pennsylvania  
bingbinl@cs.cmu.edu, {ash.jordan, goel.surbhi, akshaykr, cyrilzhang}@microsoft.com

## Abstract

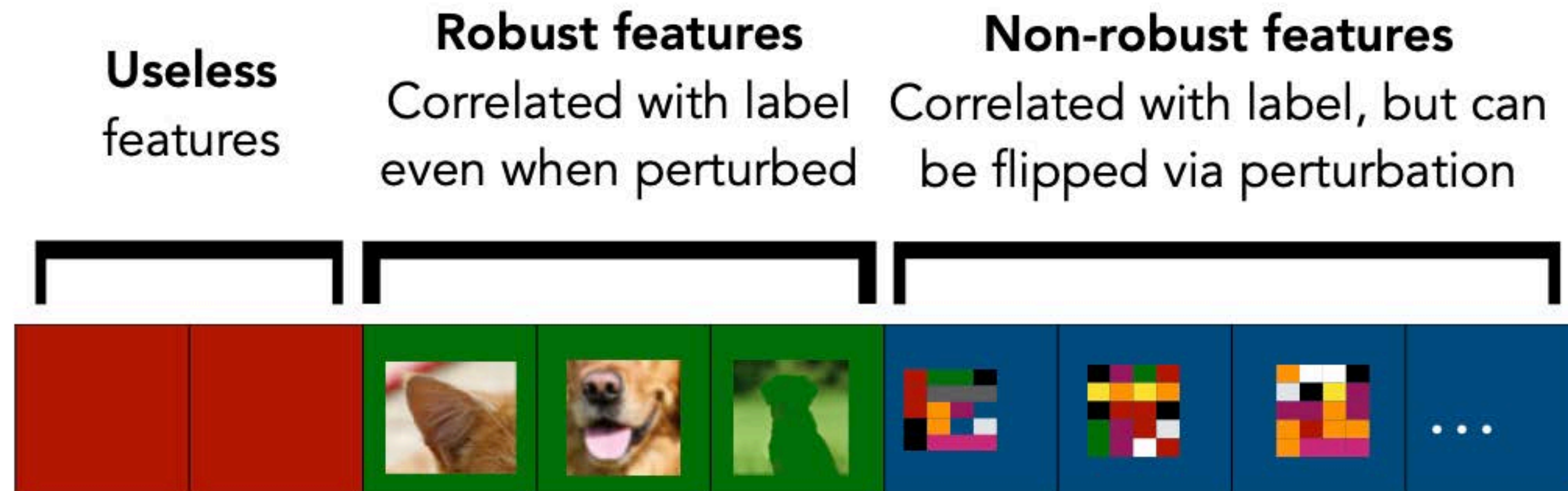
Algorithmic reasoning requires capabilities which are most naturally understood through recurrent models of computation, like the Turing machine. However, Transformer models, while lacking recurrence, are able to perform such reasoning using far fewer layers than the number of reasoning steps. This raises the question: *what solutions are these shallow and non-recurrent models finding?* We investigate this question in the setting of learning automata, discrete dynamical systems naturally suited to recurrent modeling and expressing algorithmic tasks. Our theoretical results completely characterize *shortcut solutions*, whereby a shallow Transformer with only  $o(T)$  layers can exactly replicate the computation of an automaton on an input sequence of length  $T$ . By representing automata using the algebraic structure of their underlying transformation semigroups, we obtain  $O(\log T)$ -depth simulators for all automata and  $O(1)$ -depth simulators for all automata whose associated groups are so-called *finite*. We conduct synthetic experiments by training Transformers to simulate a wide variety of automata. We find that shortcut solutions can be learned via standard training. We further investigate these solutions and propose potential mitigations.

**parallel solutions generalize within-distribution,  
but not out-of-distribution**





# Effect of adversarial training



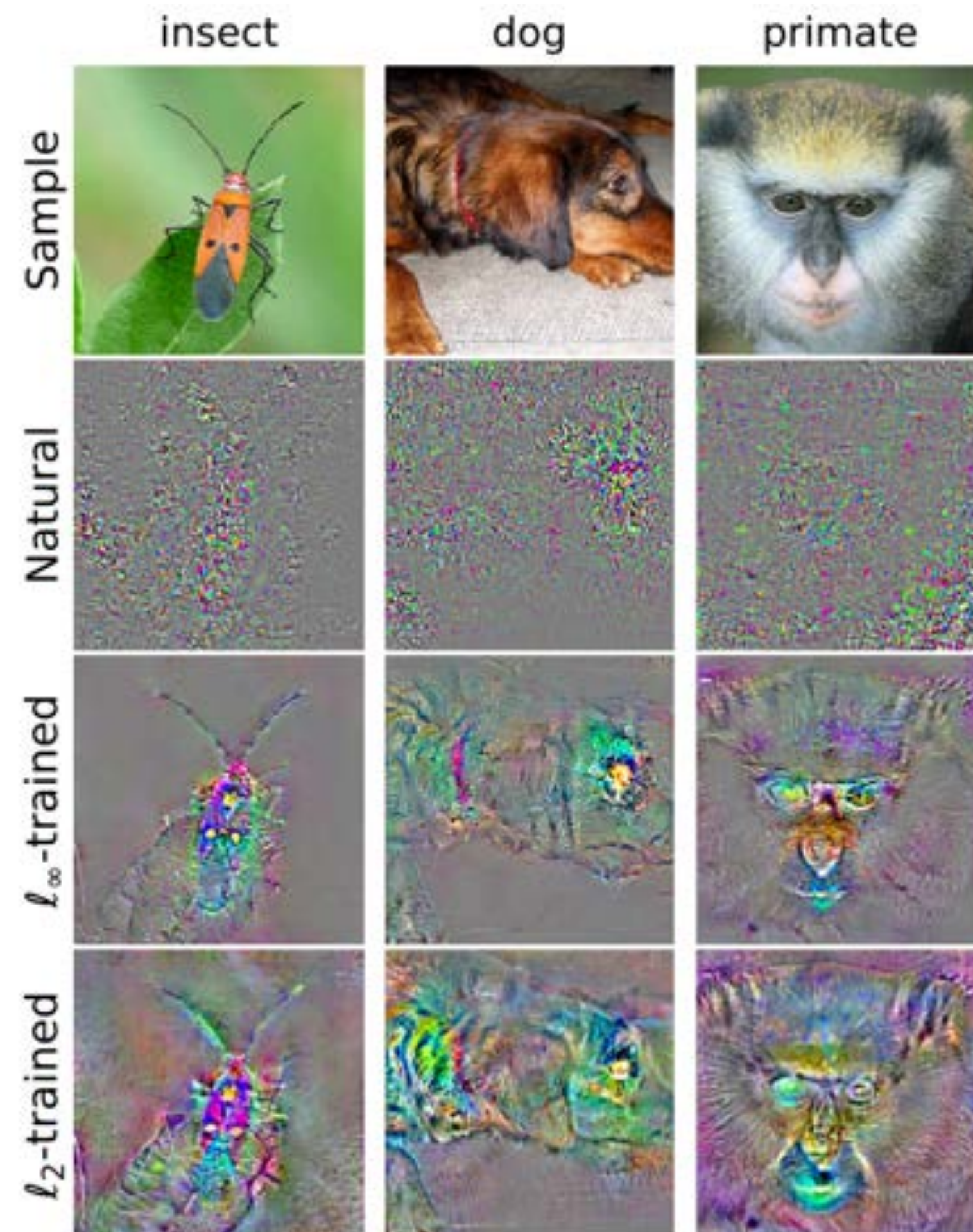
- model output should be stable under adversarial perturbations  
=> teaches **invariance to non-robust features**



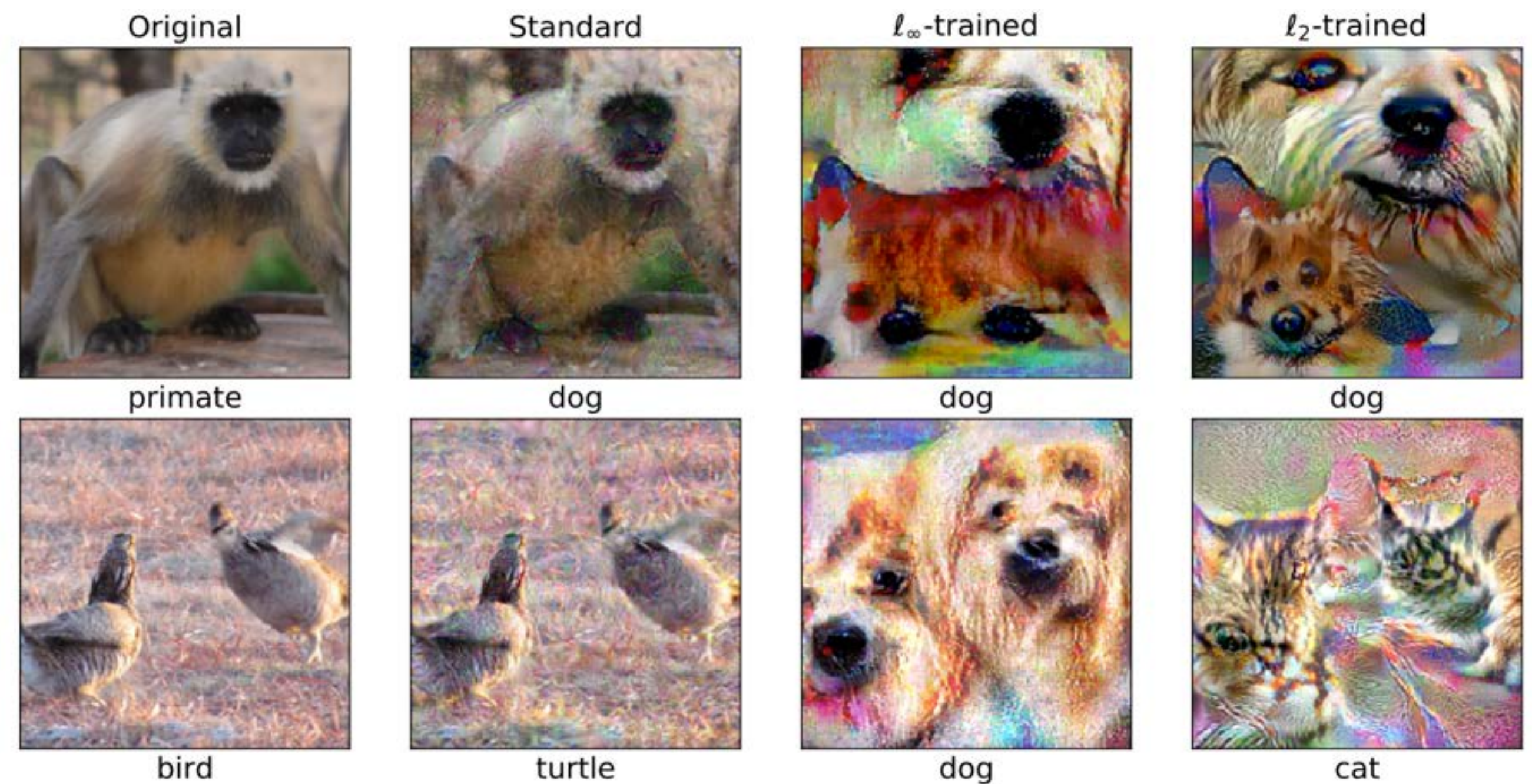
# Effect of adversarial training

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Loss gradients with respect to input pixels (most important features) show: robust model relies less on “non-robust” features, and more on human-intuitive features



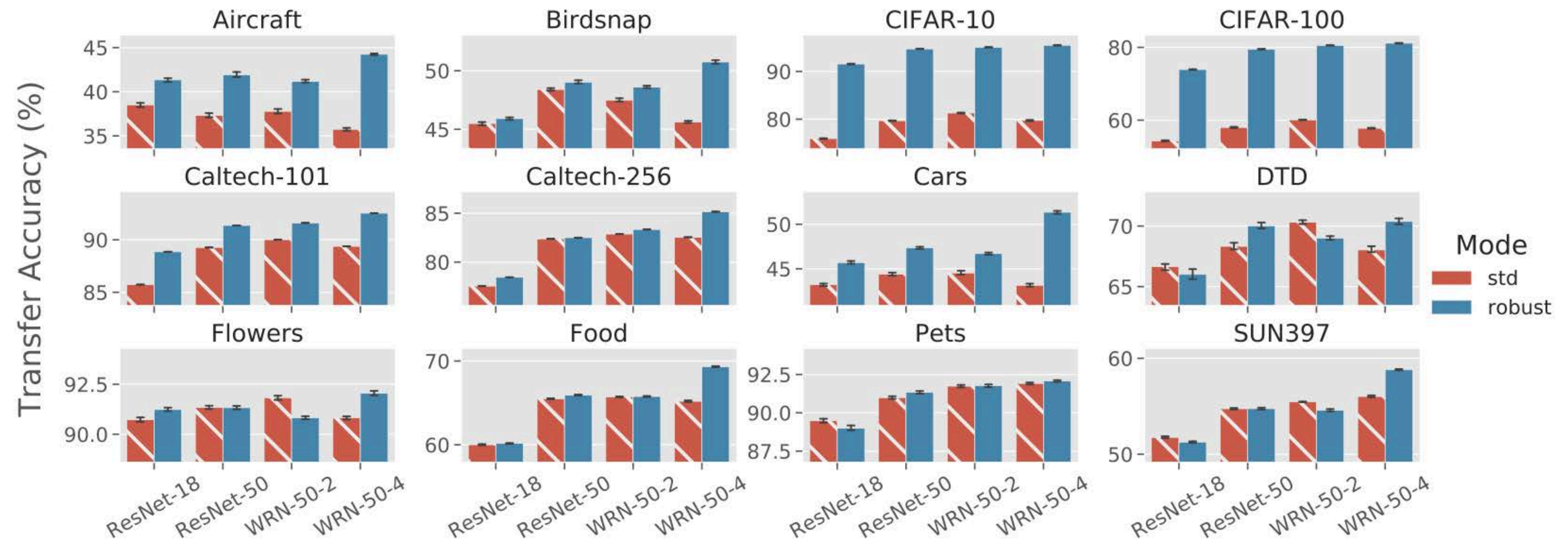
**Adversarial examples for standard and robust models**





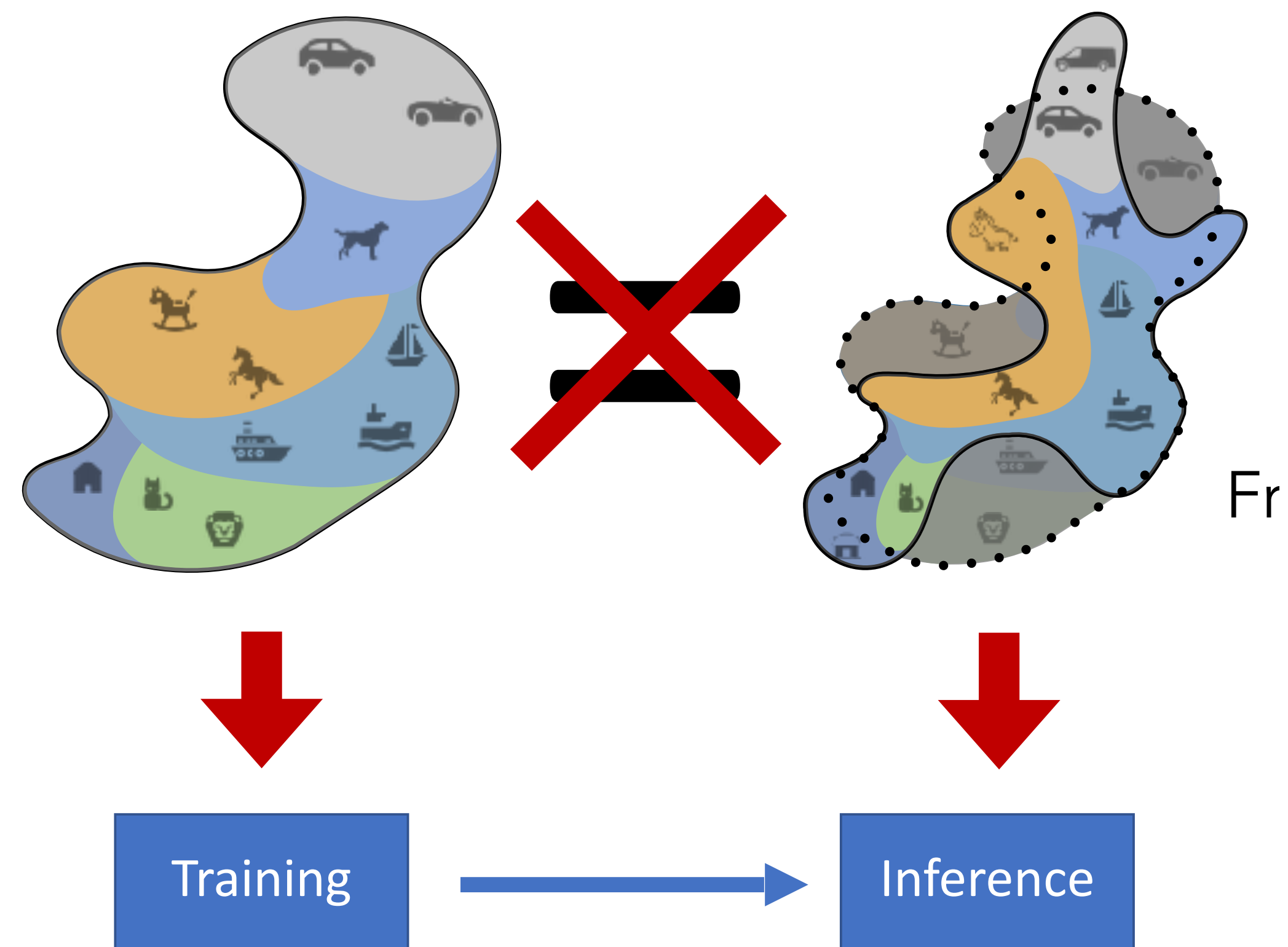
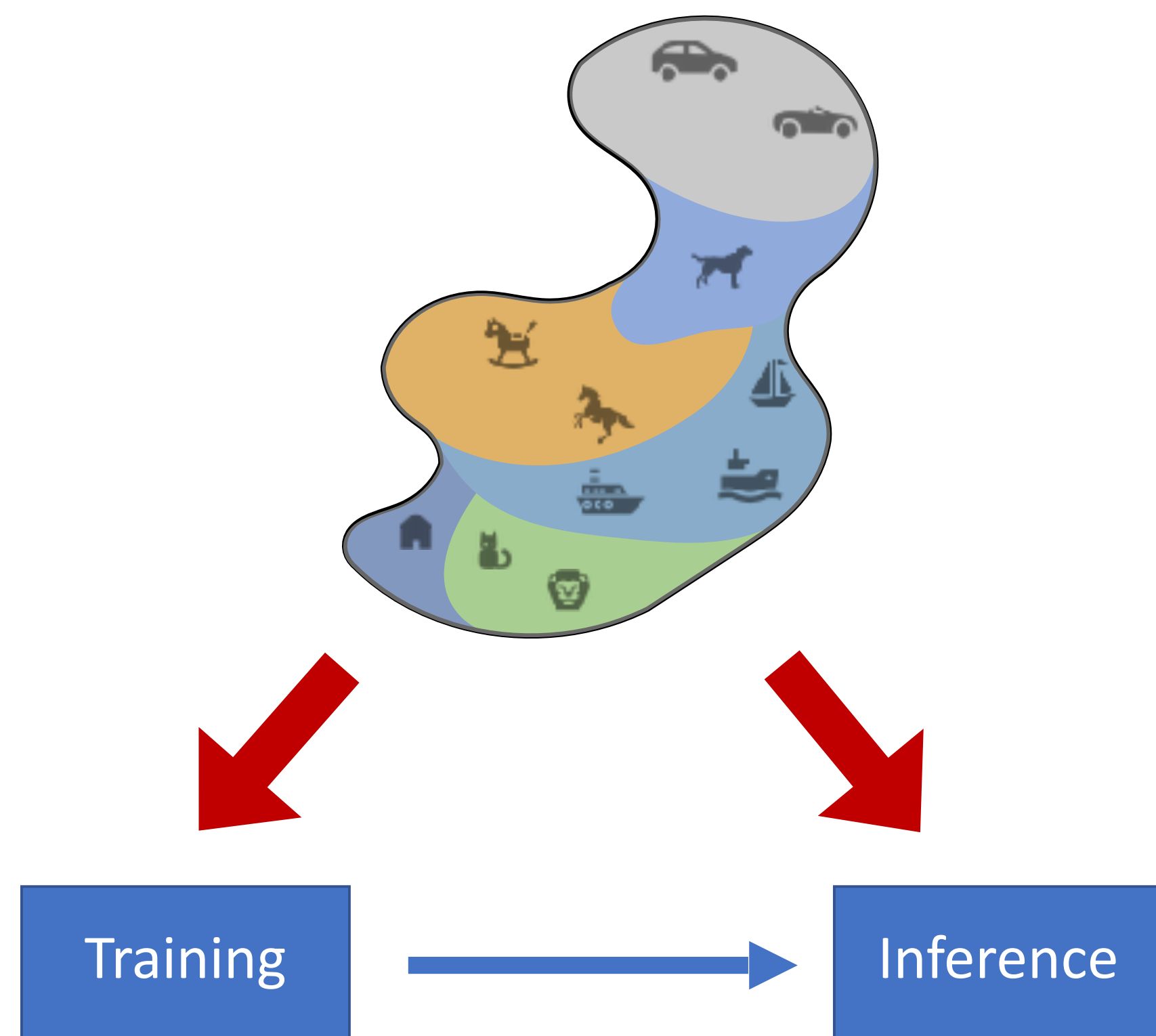
# Effect of adversarial training: transfer learning

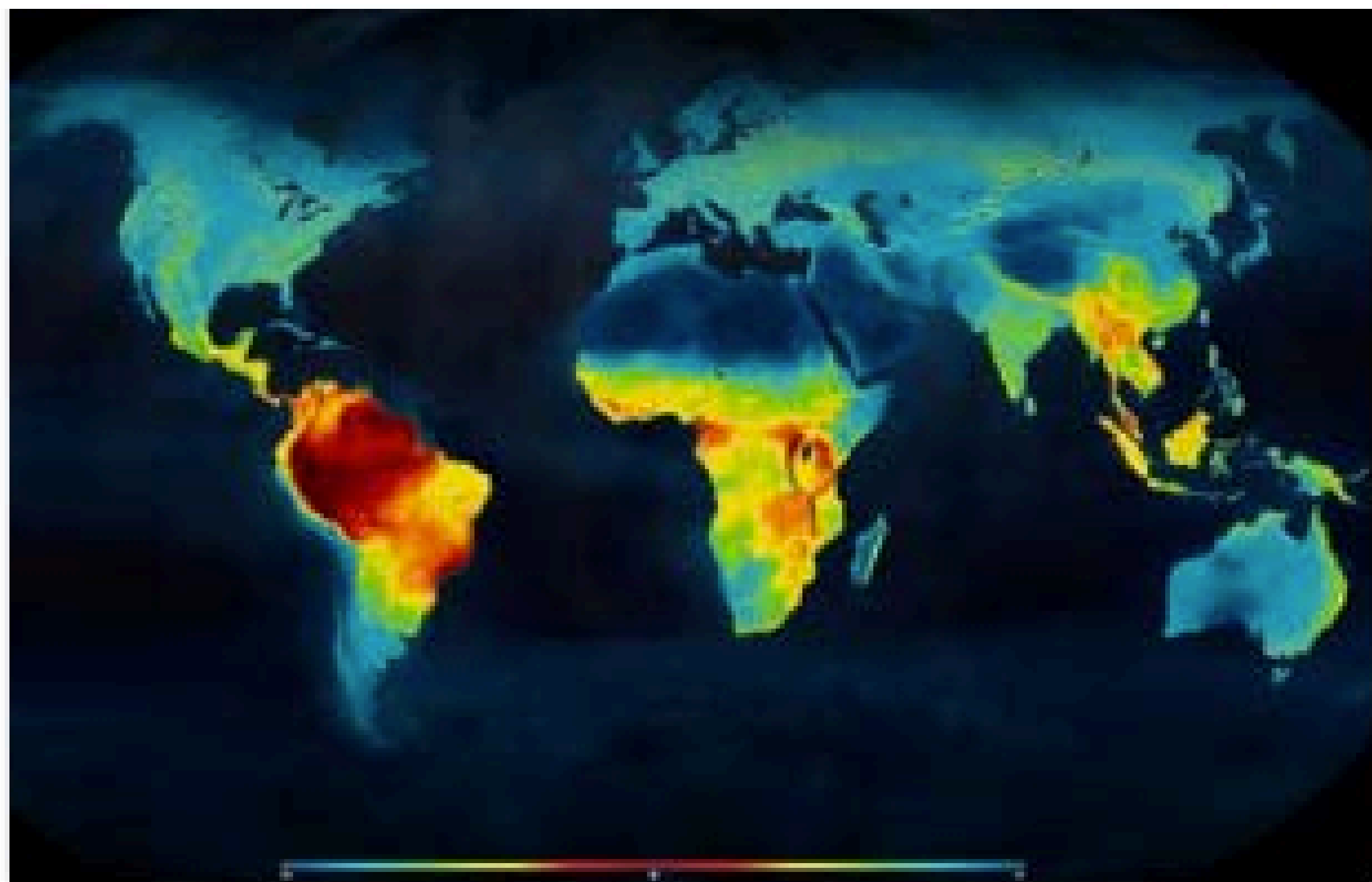
- adversarially trained models transfer better to other datasets



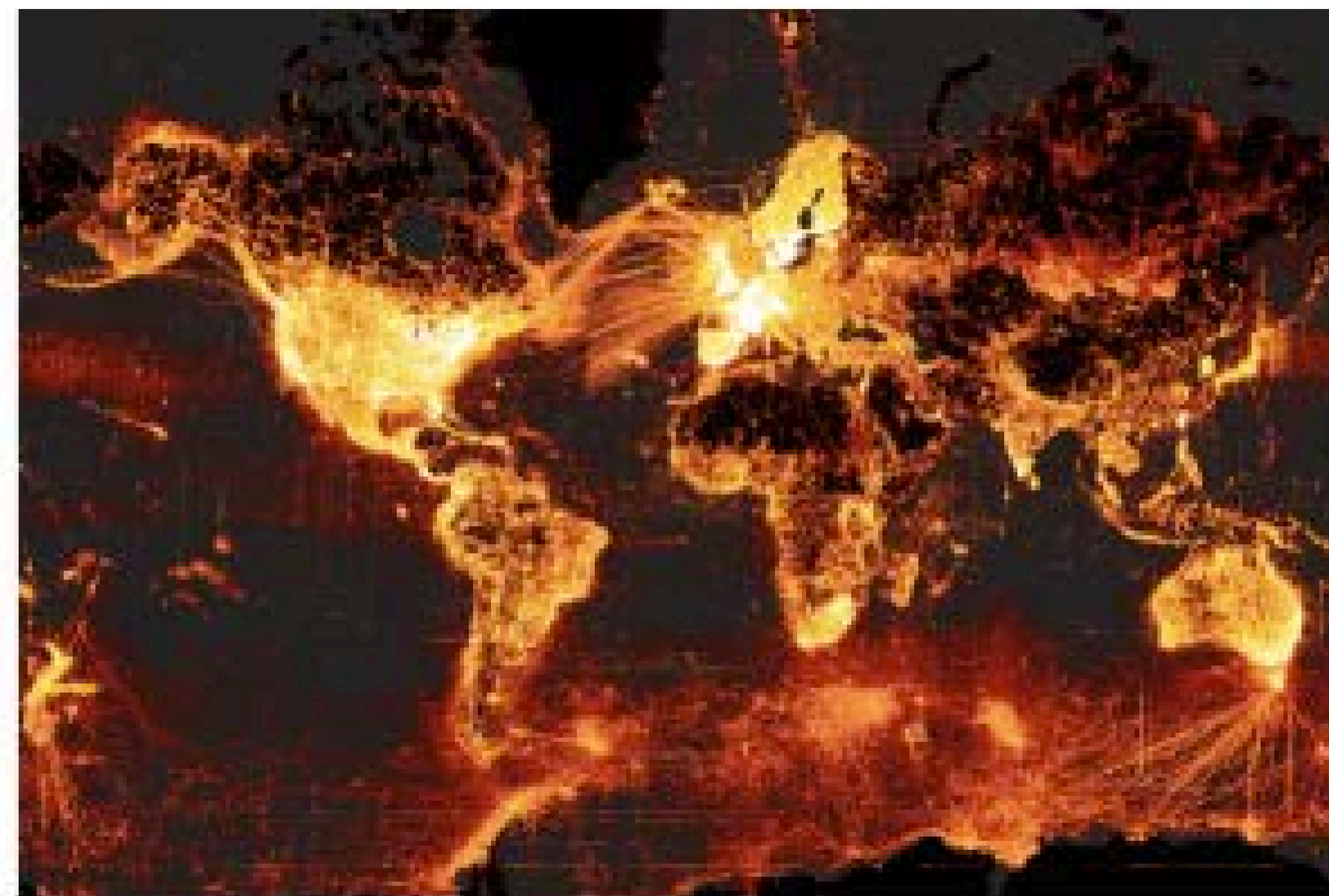
# Distribution shifts







**Map of global  
biodiversity**



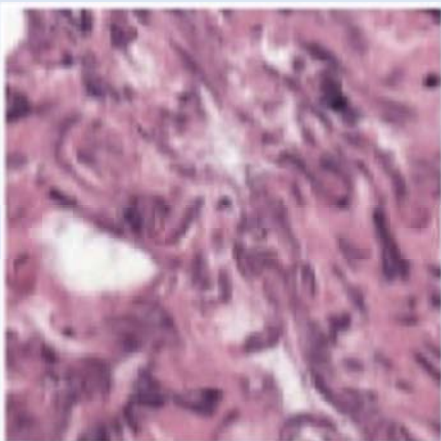


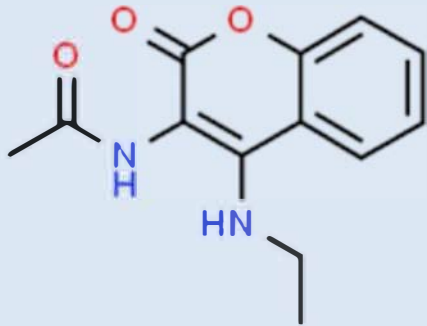
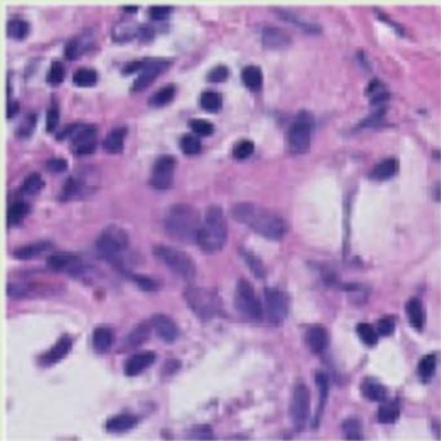


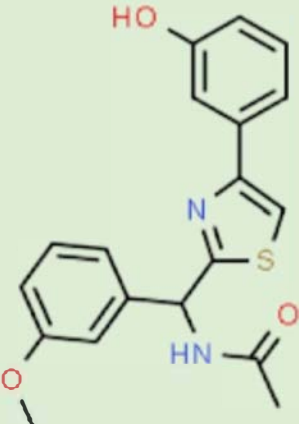
**Species occurrence  
data in GBIF**

Left: Courtesy of Mannion et al. Used under CC BY. Right: Courtesy of Sara Beery. Used under CC BY.



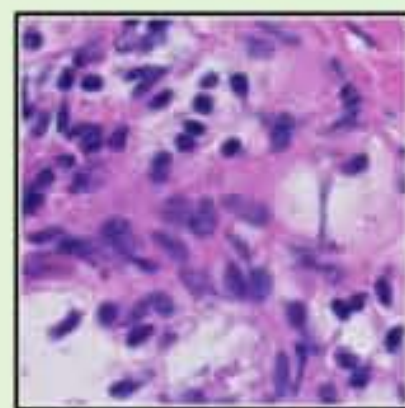
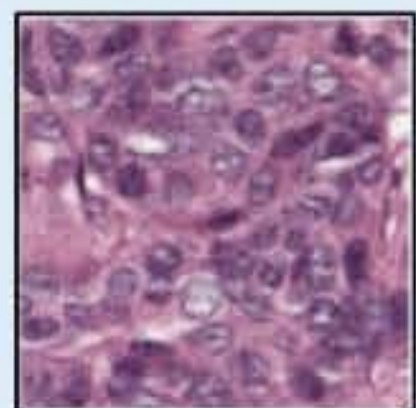
# WILDS

Pang Wei Koh\*, Shiori Sagawa\*, Henrik Marklund, Sang Michael Xie, Marvin Zhang, Akshay Balsubramani, Weihua Hu, Michihiro Yasunaga, Richard Lanus Phillips, Sara Beery, Jure Leskovec, Anshul Kundaje, Emma Pierson, Sergey Levine, Chelsea Finn, and Percy Liang

	Camelyon17	iWildCam	PovertyMap	FMoW	Amazon	CivilComments	OGB-MolPCBA
Shift	Hospitals	Locations	Countries	Time	Users	Demographics	Scaffold
Train					Overall a solid package that has a good quality of construction for the price.	What do Black and LGBT people have to do with bicycle licensing?	
Test					I *loved* my French press, it's so perfect and came with all this fun stuff!	As a Christian, I will not be patronizing any of those businesses.	
Adapted from	Bandi et al. 2018	Beery et al. 2020	Yeh et al. 2020	Christie et al. 2018	Ni et al. 2019	Borkan et al. 2019	Hu et al. 2020



### shifts across hospitals in histopathology



ID accuracy **-22.9%** OOD accuracy  
93.2%  $\longrightarrow$  70.3%

### shifts across time in satellite imagery



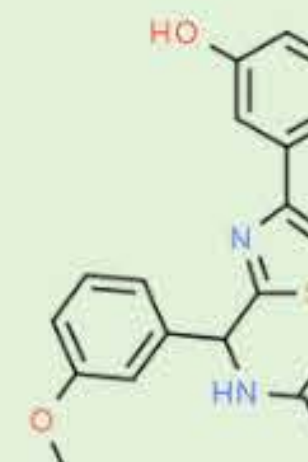
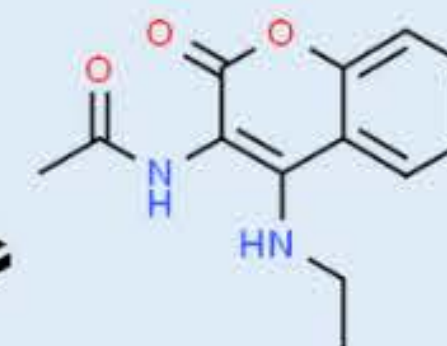
ID accuracy **-16.3%** OOD accuracy  
48.6%  $\longrightarrow$  32.3%

### shifts across regions in wheat head detection



ID accuracy **-13.7%** OOD accuracy  
63.3%  $\longrightarrow$  49.6%

### shifts across scaffold in bioassay prediction



ID AP **-7.2%** OOD AP  
34.4%  $\longrightarrow$  27.2%

[Koh et al., 2021]



## Training data

Camera 1



Camera 2



...

Camera 245



## Out-of-distribution (OOD) test data

Camera 246



...

## Control: In-distribution (ID) test data

Camera 1



Camera 2



...

Camera 245



Macro F1

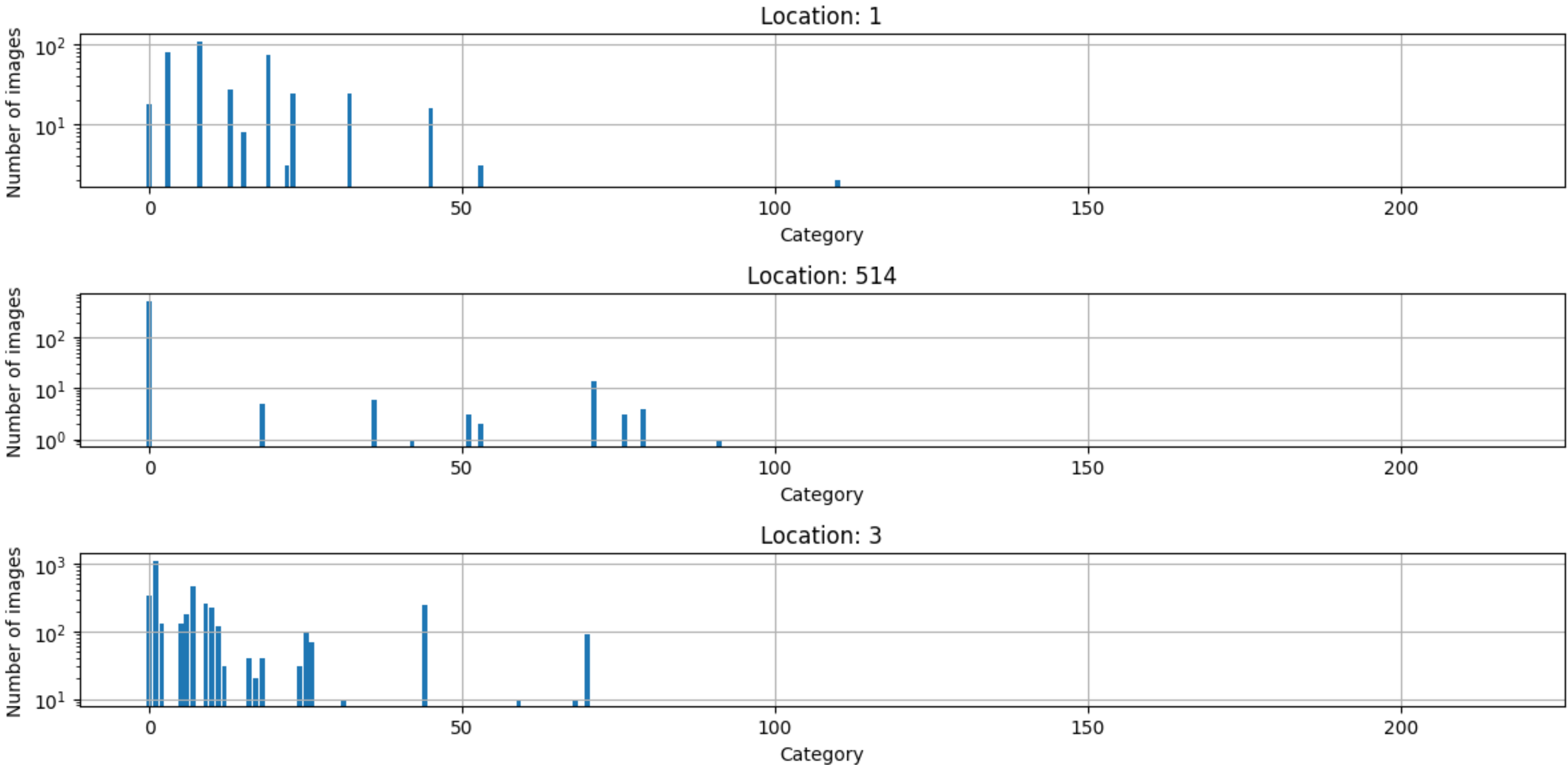
ID **-16.0%** OOD  
47.0% → 31.0%

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[Beery et al., 2020; Koh et al., 2021]

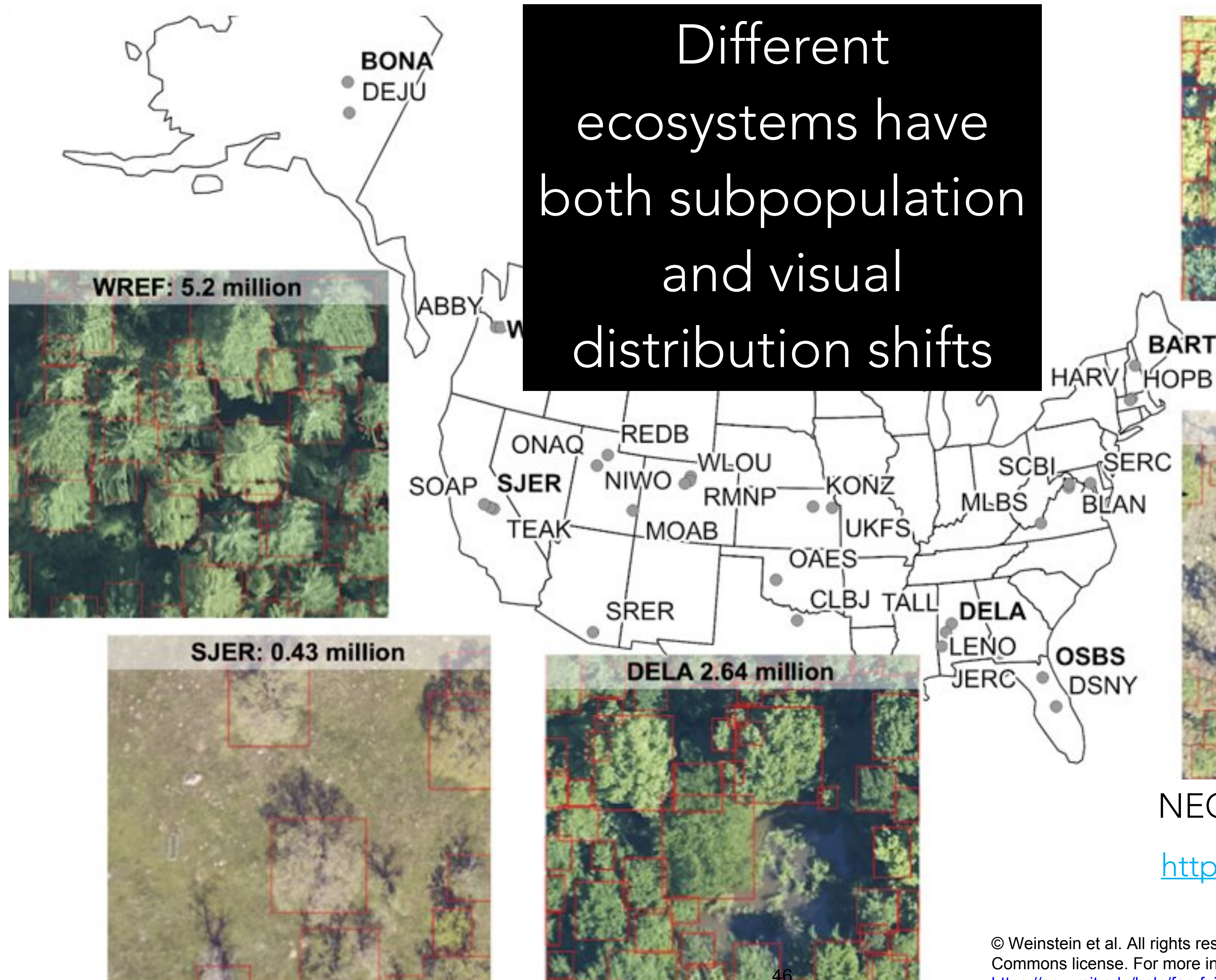


# Class distribution is different for each static sensor location





Different  
ecosystems have  
both subpopulation  
and visual  
distribution shifts



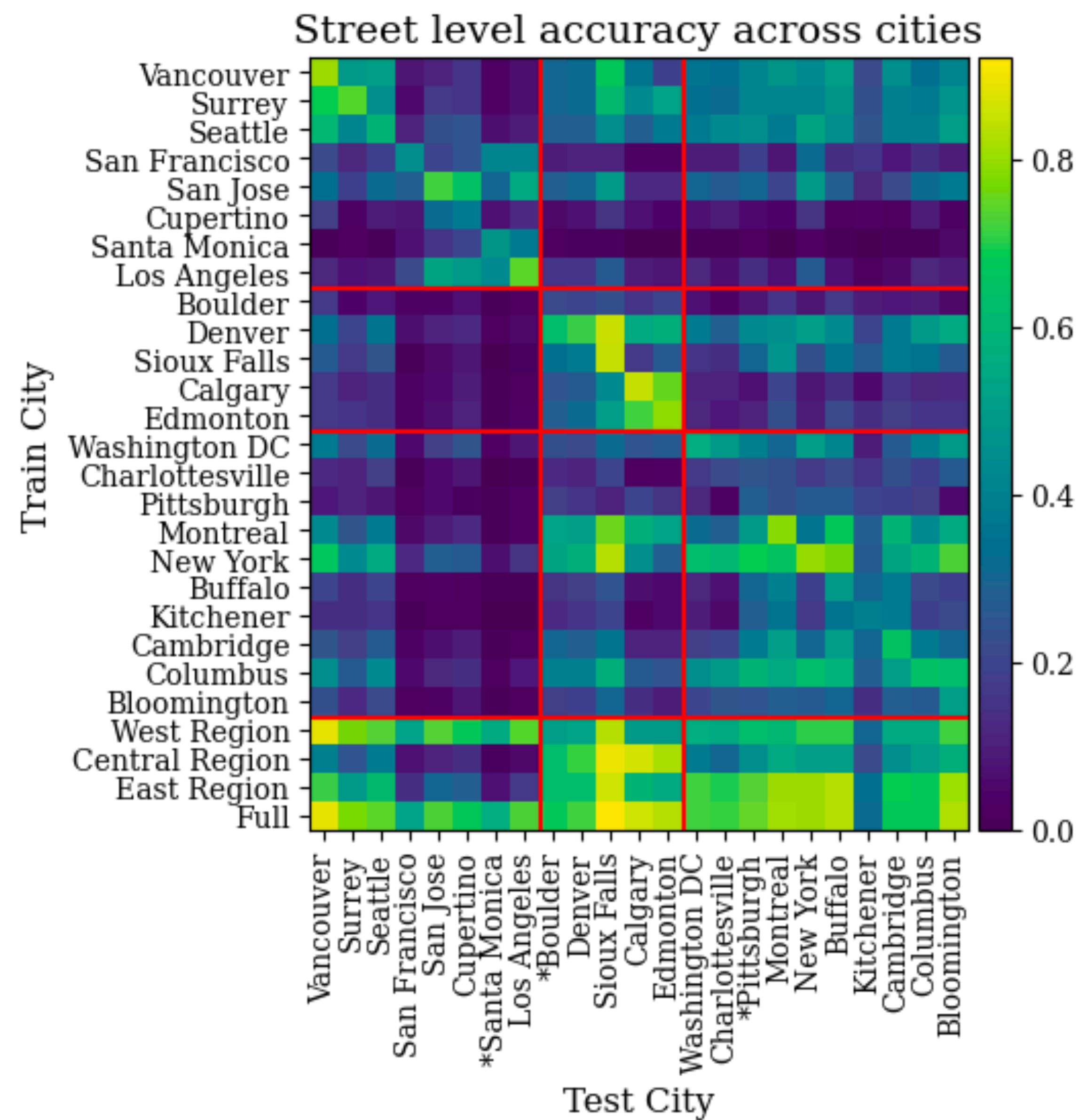
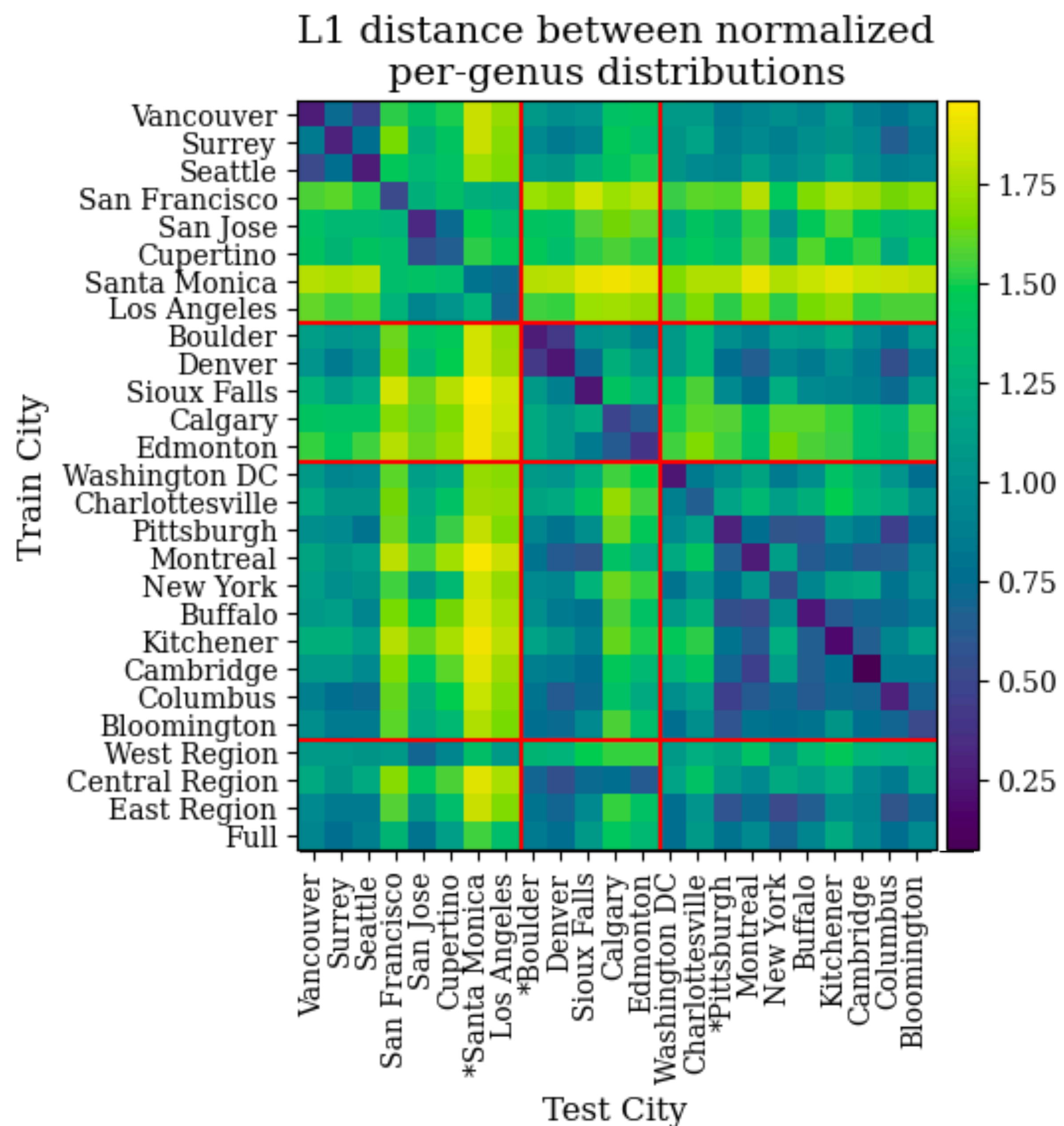
NEONCROWNS Dataset

<http://visualize.idtrees.org/>

Weinstein et al., 2020



# Performance has strong correlation with subpop. distribution similarity



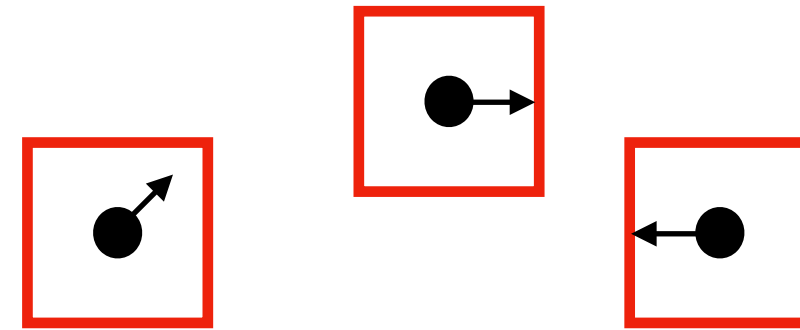


# What to do about distribution shift?

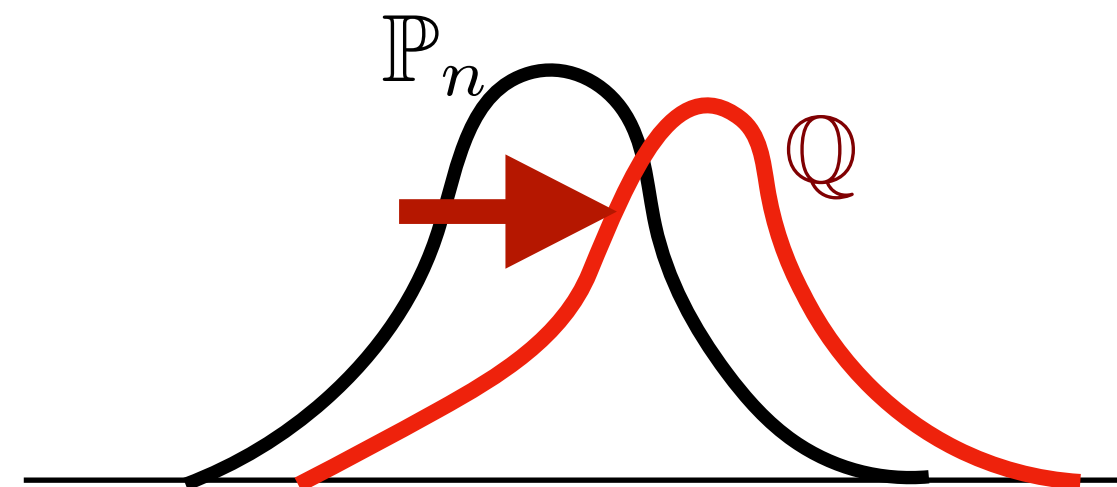


# One path: distributionally robust optimization

- So far: allowed to perturb each datapoint by a limited amount



- Alternative: we can perturb the entire training distribution (sample) by a certain amount, together





# Distributionally robust optimization

- Standard training:  $\frac{1}{n} \sum_{i=1}^n \text{Loss}(f_{\theta}(\mathbf{x}^{(i)}), y^{(i)}) = \mathbb{E}_{(\mathbf{x}, y) \sim \mathbb{P}_n} [\text{Loss}(f_{\theta}(\mathbf{x}), y)]$

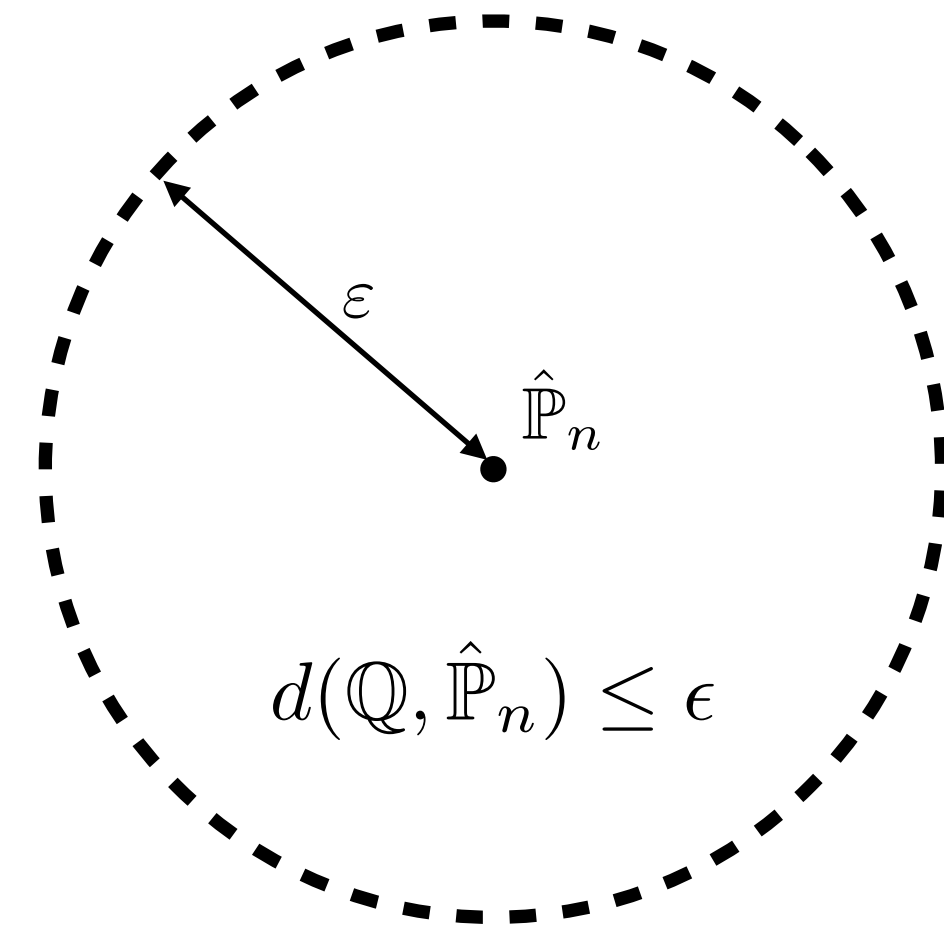
**allow a small  
perturbation of  
training sample  
(discrete distribution)**

- Distributionally robust optimization (DRO):

$$\min_{\theta} \max_{\mathbb{Q}, D(\mathbb{Q}, \mathbb{P}_n) < \epsilon} \mathbb{E}_{(\mathbf{x}, y) \sim \mathbb{Q}} [\text{Loss}(f_{\theta}(\mathbf{x}), y)]$$

**e.g. re-weight or  
perturb training data points**

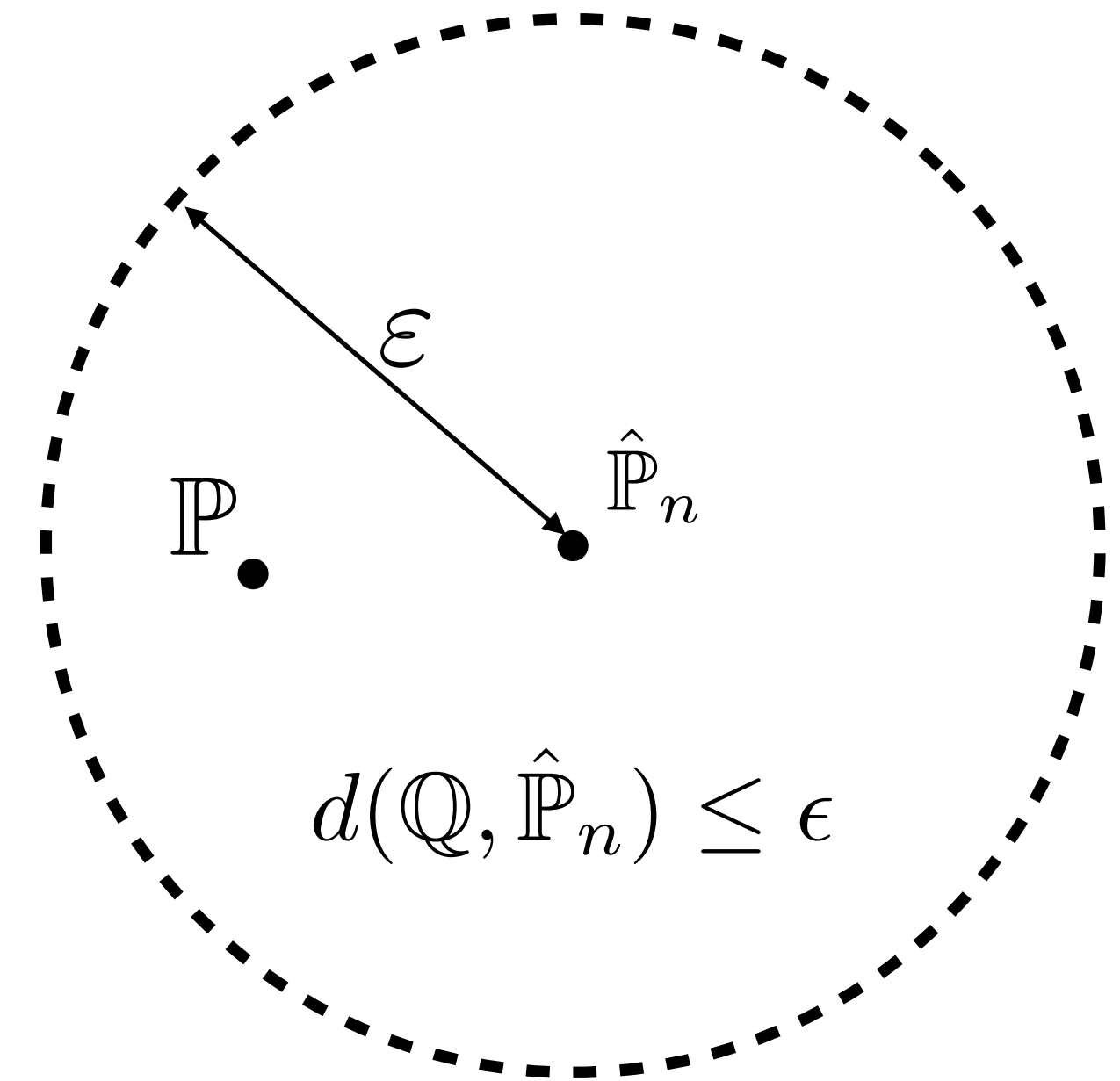
- Various choices of measuring “distance” between probability distributions:  $\chi^2$ -distance, Wasserstein distance, maximum mean discrepancy (MMD)...



# DRO and generalization

$$\min_{\theta} \max_{\mathbb{Q}, D(\mathbb{Q}, \mathbb{P}_n) < \epsilon} \mathbb{E}_{(\mathbf{x}, y) \sim \mathbb{Q}} [\text{Loss}(f_{\theta}(\mathbf{x}), y)]$$

- DRO optimizes for a set of training data sets/distributions
- Say underlying data distribution is  $\mathbb{P}$
- Empirical training data is  $\hat{\mathbb{P}}_n$
- If  $D(\mathbb{P}, \hat{\mathbb{P}}_n) < \epsilon$ , then we are guaranteed to perform well on  $\mathbb{P}$  too, i.e., generalize!





# Application: DRO and class imbalance

- Assume population has K sub-groups (example: K=2).
- Usually: minimize “Empirical Risk” (average error)

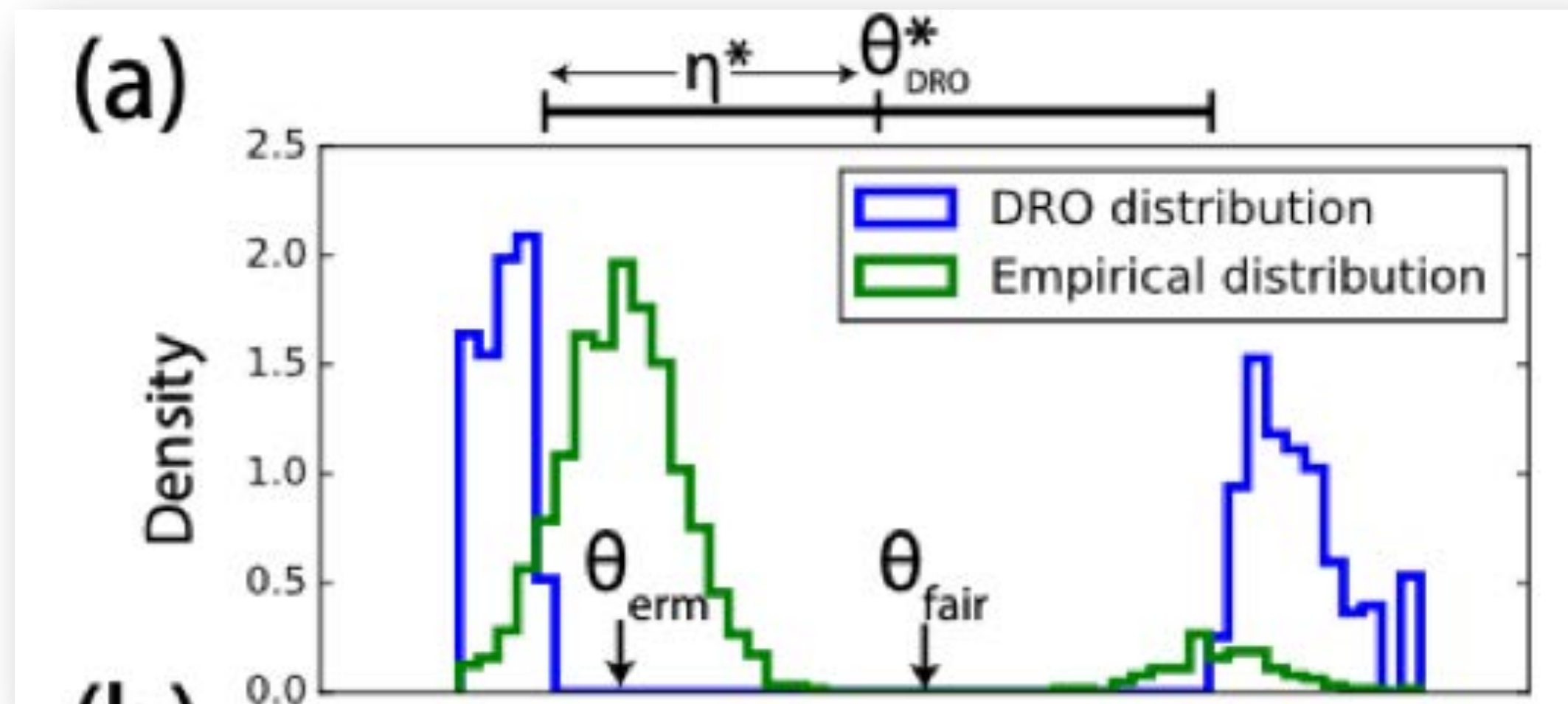
$$\min_{\theta} \frac{1}{n} \left( \underbrace{\sum_{i \text{ in group 1}} \text{Loss}(x_i; \theta)}_{80\%} + \underbrace{\sum_{j \text{ in group 2}} \text{Loss}(x_j; \theta)}_{20\%} \right)$$

- Here, 50% error on minority group makes only 10% average error.  
(+ statistical patterns for minority may be different)
- We can “ignore” minority group and still get decent loss!

# DRO and class imbalance

- Idea: automatically re-weight data via DRO  
=> pay more attention to minority class

$$\min_{\theta} \max_{\mathbb{Q}, D(\mathbb{Q}, \mathbb{P}_n) < \epsilon} \mathbb{E}_{(\mathbf{x}, y) \sim \mathbb{Q}} [\text{Loss}(f_{\theta}(\mathbf{x}), y)]$$





# What to do about distribution shift?

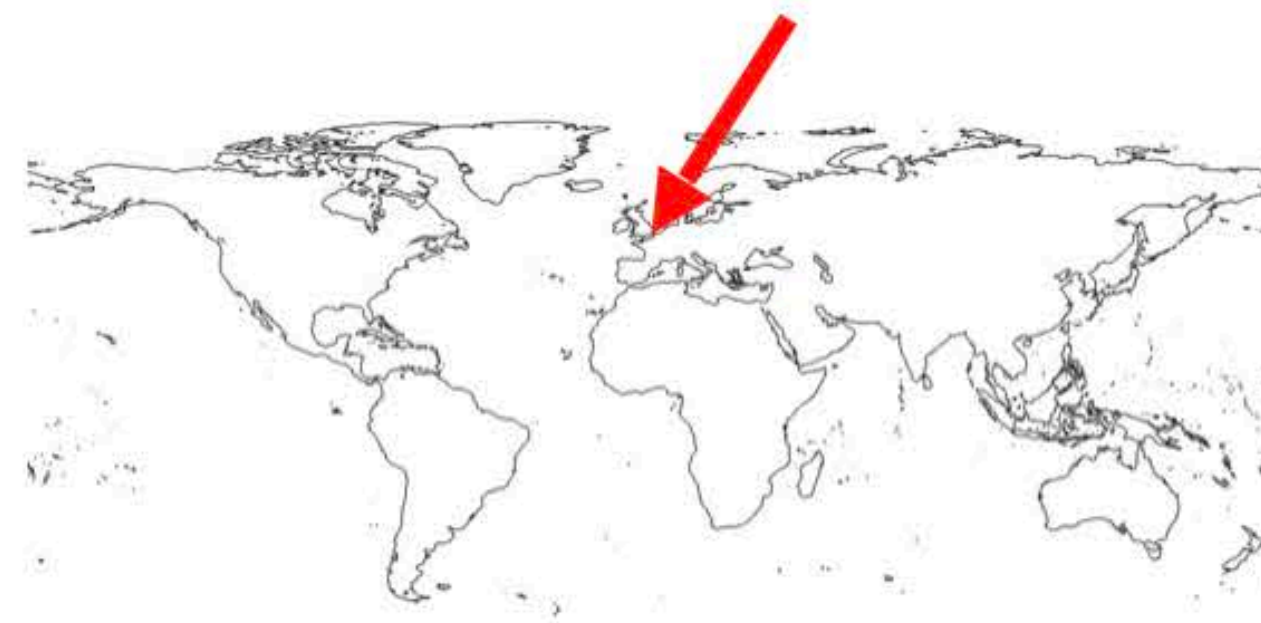
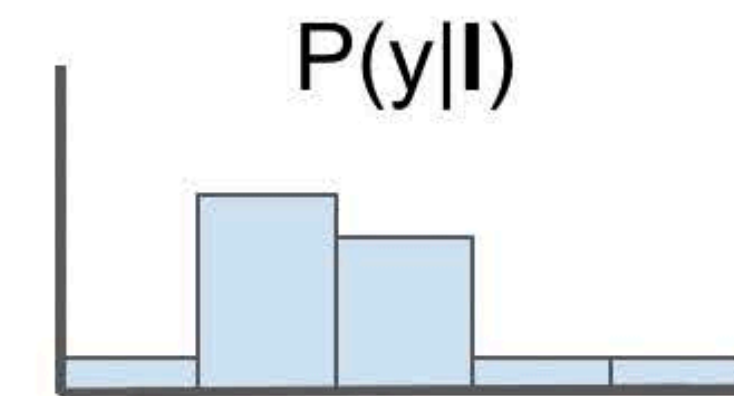
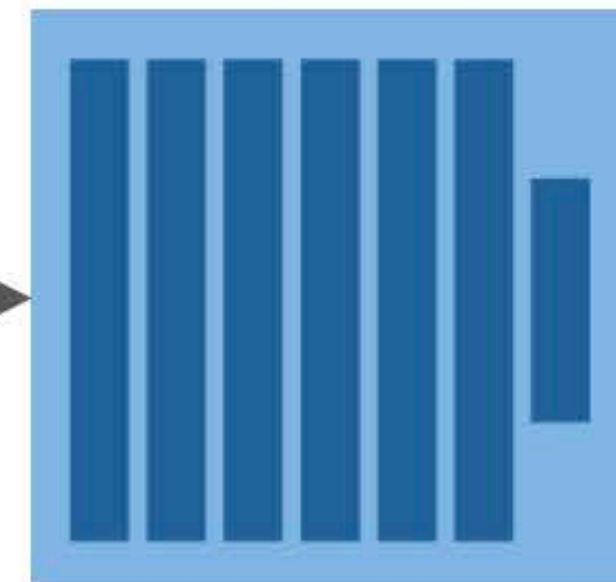
- Distributionally robust optimization

# Learn a spatiotemporal prior

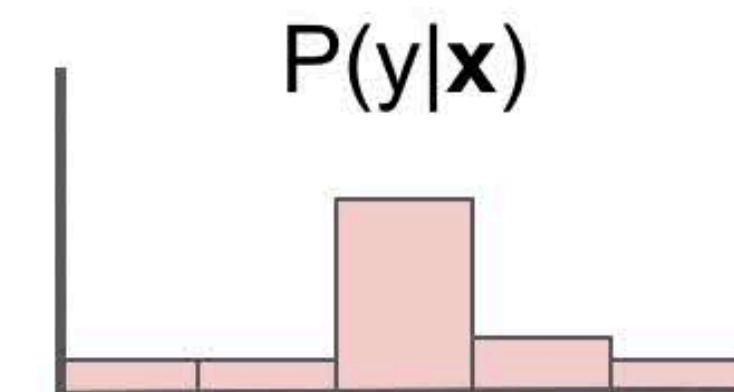
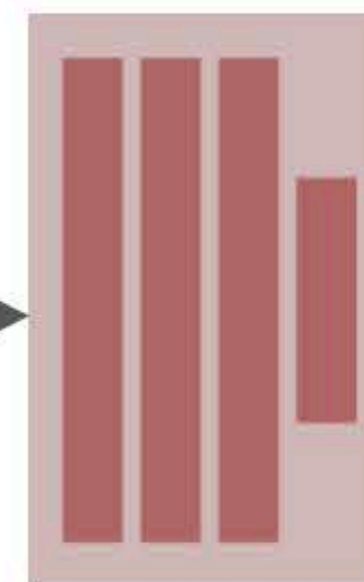
$$P(y|I, \mathbf{x}) \propto P(y|I)P(y|\mathbf{x})$$



Image Classifier



Spatio-Temporal Prior



Combine

$\mathbf{x} = (\text{longitude, latitude, day})$


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# What to do about distribution shift?

- Distributionally robust optimization
- Learn (or use) a prior for subpopulation shift



Domain  
  
 Adaptation



Source domain: ● ★ ▲ ■

Target domain: □ △ ○ ☆

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# What to do about distribution shift?

- Distributionally robust optimization
- Learn (or use) a prior for subpopulation shift
- Domain adaptation (next lecture!)



Original Plates



ImageNet

Acquiring images of plates with utensils



Bing

Stable Diffusion

ImageNet\*



Figure 8: Real images of plates, with and without food and either on a table or in the grass. Below each image is the predicted class by an ImageNet-trained ResNet50.

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# What to do about distribution shift?

- Distributionally robust optimization
- Learn (or use) a prior for subpopulation shift
- Domain adaptation (next lecture!)
- Diagnose failures

# What to do about distribution shift?

- Distributionally robust optimization
- Learn (or use) a prior for subpopulation shift
- Domain adaptation (next lecture!)
- Diagnose failures
- Get training data that is representative of your test domain  
(works better than any algorithm)



# Summary

- Out-of-distribution generalization: big challenge, but helps understand what NNs learn.
  - Adversarial examples and training
  - Distribution shifts

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