

**Recitation 3 Notes:**  
**30 September, 2022**

**Reminders:**

- **MQ4 next Wednesday 10/5**
- **PS1 due next Wednesday**

**Lecture 4 Recap: Simple Programs, Intro to Binary Numbers**

1. *Simple Programs*
  - Guess-and-check algorithms are one way to find a solution to a problem through exhaustive enumeration.
  - Guess solution -> evaluate guess -> make educated adjustment to the guess and **repeat ....**
  - Repeat these steps until you find a solution or have exhausted your set of possible solutions.
  - Example programs: Guessing Square or Cube roots.
2. *Intro to Binary Numbers*
  - Computers use binary numbers.
  - Everything is stored in one of two states – either 0 or 1.
  - Binary numbers are efficient and easy to perform operations on.
  - A sequence of binary numbers e.g 00110011 is called a **sequence of bits**.
  - Base 10 numbers can be converted to Binary numbers and visa versa.

First eight bits are the powers of two:

128, 64, 32, 16, 8, 4, 2, 1

So, in the first 8 bits we can store number up to (but not including) 256.

Example: Convert base 10 number 56 into binary representation.

56 = 00111000

Example2: Convert 00011001 into base 10.

$00011001 = 1*1 + 1*8 + 1*16 = 25$

**Lecture 5 Recap: Floats, Fractions and Approximation Algorithms**

1. *Floats*
  - Python uses “floating points” to approximate real numbers.
  - Operations on floats introduce a very small error.
  - Many smaller errors turn into a bigger error.
2. *Fractions & Approximation*
  - We use the same idea to store fractions in binary by raising 2 to the power of some negative number.

Ultimately, a computer represents everything in bits. So, numbers with many digits trailing the decimal are often approximated.

As a result, be careful when comparing and working with floats.

### 3. *Approximation Algorithms*

- Like guess and check but the goal is to find an answer that is considered “good enough”, and not necessarily exact.
- Guess an answer -> check if it’s “good enough” -> if not, make an educated change your guess -> repeat until your guess is “good enough”
- Key parameters: increment, epsilon, number of guesses etc...
- Remember to keep in mind what happens if you overshoot the close-enough stopping condition – don’t want an infinite loop.

## Lecture 6 Recap: Bisection Search, Newton-Raphson

### 1. Bisection Search

- Search algorithm applied to problems with an inherent order to the range of possible answers (e.g an ordered list of numbers).
- Step to a simple binary search algorithm:
  - Guess the midpoint of the interval
  - If not the answer, check if answer is greater or less than the midpoint
  - Change interval
  - Repeat
- This method cuts the set of possible answer to check in half at each stage → logarithmic growth characteristic → more efficient algorithm

### 2. Newton-Raphson

- General approximation algorithm to find the roots of a polynomial in one variable
- Given polynomial function  $p(x)$ , the goal is to solve for  $r$  such that  $p(r) = 0$ .
- N-R showed that:
  - If  $g$  is an approximation to the root,  $r$ , then
$$g - p(g)/p'(g)$$
is a better approximation, where  $p'$  is the derivative of  $p$ .

## Lecture 7: Functions and Scope

### Functions

- Functions capture computation within a black box.
- They allow us to reuse code and write programs in a more concise way.
- Functions take in input and return outputs.
- Inputs are passed as parameters of the function and outputs are returned using the return statement.
- Calling a function  
`My_output = function_name(arg1, arg2, ..., argN)`
- When called, the entire function is replaced with the return value
- **print vs return**
  - **print:** for the user, just displays a value
  - **return:** for the computer and allows you to send values in a function back to other parts of your code
    - Nothing in the function will be executed after a return statement is executed.
    - Python’s default **return** is **None**.

### Scope

- Variable assignments are tracked in a **symbol table** or **stack frame** that maps variable names to their values
- When a function is **called**, a new stack frame is created.
- When the function returns, the stack frame pops off/is destroyed
- My python tutor does a good visualization of this <https://pythontutor.com/>.

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<https://ocw.mit.edu>

6.100L Introduction to CS and Programming Using Python  
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